

# Crypto

## Part 2 of 3

CMSC 23200/33250, Winter 2020, Lecture 4

---

David Cash & Blase Ur

University of Chicago

# Tool to address key-length of OTP: Stream Ciphers

Stream cipher syntax: Algorithm  $G$  that takes one input and produces an very long bit-string as output.

Usually very, very large  
(petabytes if needed)

Key/Seed  $k$ : 1100...11

Typically 16 or 32 bytes.



$G(k)$ : 11111010001000111010100101000101100100111100...

$\oplus$  0010001001111010111011011100001010100111000...

Use  $G(\text{seed})$  in place of pad.

Still malleable and still one-time, but key is shorter.

# Addressing pad reuse: Stream cipher with a nonce

Stream cipher with a nonce: Algorithm  $G$  that takes **two inputs** and produces a very long bit-string as output.

<u>Nonce IV:</u>	<u>Key/Seed <math>k</math>:</u>
1100...11	1100...11

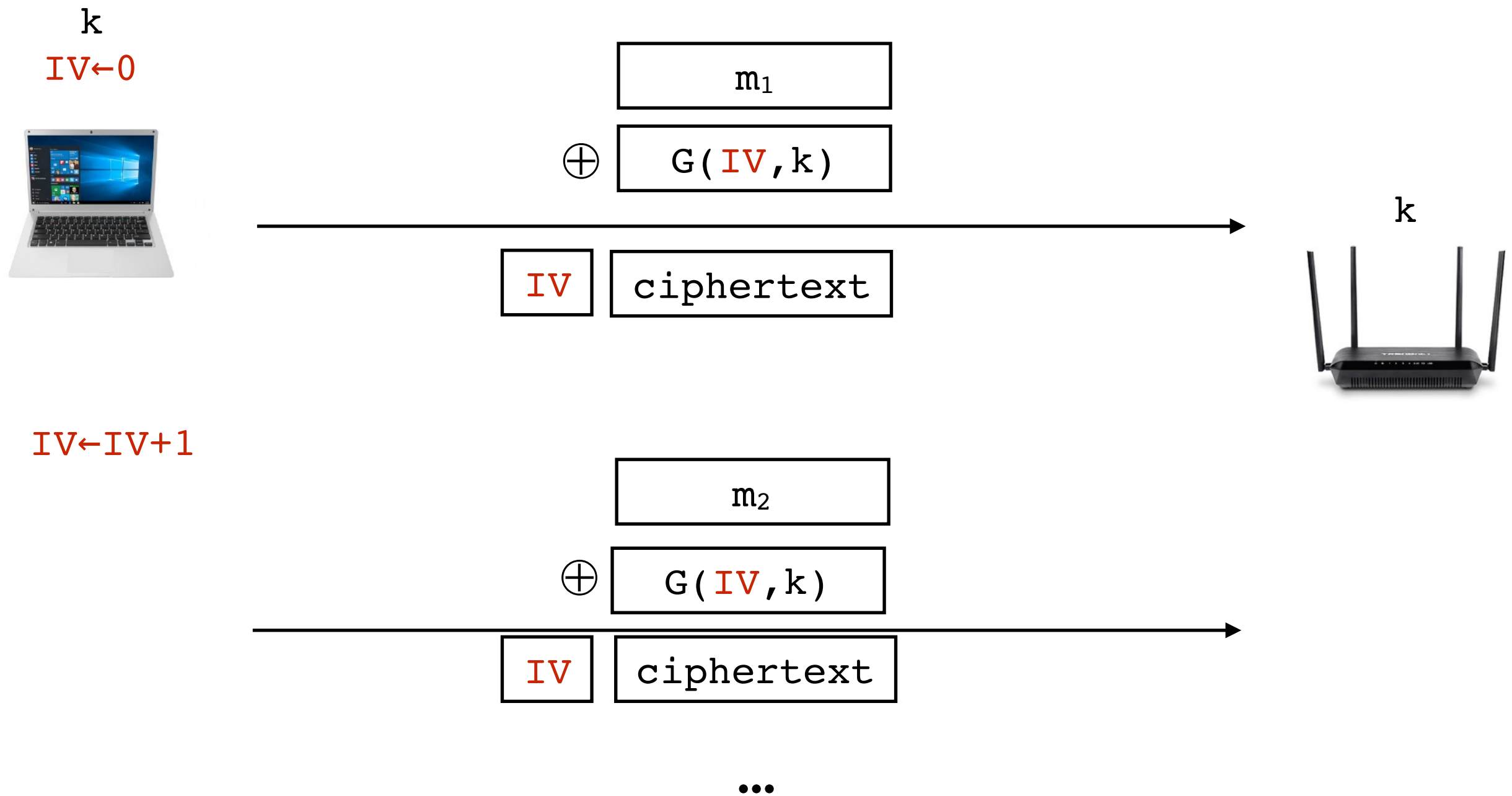


$G(IV, k)$ : 11111010001000111010100101000101100100111100...

- “nonce” = “number once”.
- Usually denoted  $IV$  = “initialization vector”

Security goal: When  $k$  is random and unknown,  $G(IV, k)$  should “look” random and independent for each value of  $IV$ .

# Solution 1: Stream cipher with a nonce



- If nonce repeats, then pad repeats

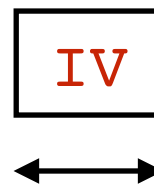
# Example of Pad Re-use: WEP



**Warning: Broken**



IEEE 802.11b WEP: WiFi security standard '97-'03



IV is 24-bit wide counter

- Repeats after  $2^{24}$  frames ( $\approx 16$  million)
- IV is often set to zero on power cycle

Solutions: (WPA2 replacement)

- Larger IV space, or force rekeying more often
- Set IV to combination of packet number, address, etc

# Example of Pad Re-use: WEP



Warning: Broken



IEEE 802.11b WEP: WiFi security standard '97-'03

- Re  
- Of

ars TECHNICA

BIZ & IT TECH SCIENCE POLICY CARS GAMING & CULTURE FORUMS

BIZ & IT —

## Serious flaw in WPA2 protocol lets attackers intercept passwords and much more

KRACK attack is especially bad news for Android and Linux users.

DAN GOODIN - 10/15/2017, 11:37 PM

Solutions: (W)

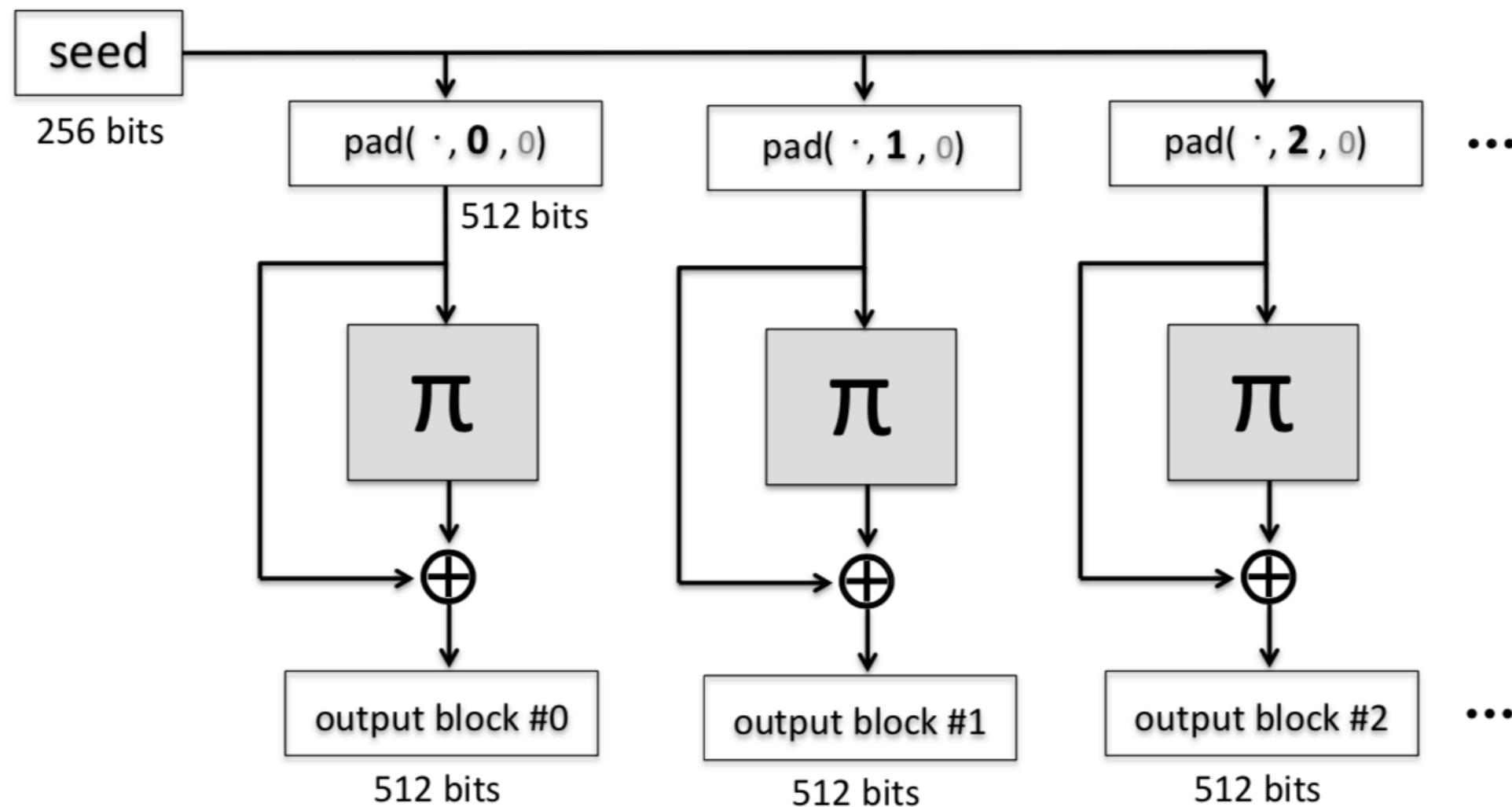
- Larger IV space

- Set IV to combination of packet number, address, etc

parameters to their initial values. KRACK forces the nonce reuse in a way that allows the encryption to be bypassed. Ars Technica IT editor Sean Gallagher has [much more about KRACK here](#).

# Example Stream Cipher w/ Nonces: ChaCha20

- Key-length: 256 bits
- Generates stream by applying a fixed permutation to seed and counter
- Uses “feed-forward” to break up permutation structure



# ChaCha20 Block Permutation

```
#define ROTL(a,b) (((a) << (b)) | ((a) >> (32 - (b))))
#define QR(a, b, c, d) (
    a += b, d ^= a, d = ROTL(d,16), \
    c += d, b ^= c, b = ROTL(b,12), \
    a += b, d ^= a, d = ROTL(d, 8), \
    c += d, b ^= c, b = ROTL(b, 7))

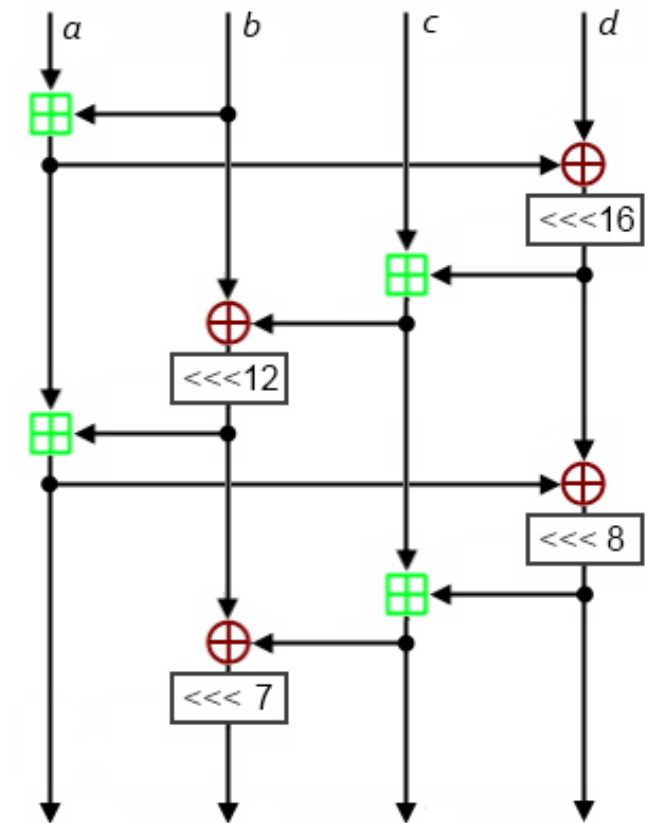
#define ROUNDS 20

void chacha_block(uint32_t out[16], uint32_t const in[16])
{
    int i;
    uint32_t x[16];

    for (i = 0; i < 16; ++i)
        x[i] = in[i];

    // 10 loops x 2 rounds/loop = 20 rounds
    for (i = 0; i < ROUNDS; i += 2) {
        // Odd round
        QR(x[0], x[4], x[ 8], x[12]); // column 0
        QR(x[1], x[5], x[ 9], x[13]); // column 1
        QR(x[2], x[6], x[10], x[14]); // column 2
        QR(x[3], x[7], x[11], x[15]); // column 3
        // Even round
        QR(x[0], x[5], x[10], x[15]); // diagonal 1 (main diagonal)
        QR(x[1], x[6], x[11], x[12]); // diagonal 2
        QR(x[2], x[7], x[ 8], x[13]); // diagonal 3
        QR(x[3], x[4], x[ 9], x[14]); // diagonal 4
    }
    for (i = 0; i < 16; ++i)
        out[i] = x[i] + in[i];
}
```

QR(a, b, c, d):



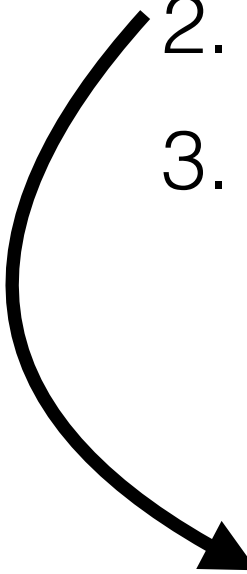
???

In Assignment 2: Develop attack when a weak “statistical” stream cipher is used.



# Issues with One-Time Pad

1. Reusing a pad is insecure ✓ *Use unique nonces*
2. One-Time Pad is *malleable*
3. One-Time Pad has a long key ✓ *Use stream cipher with short key*



More difficult to address; We will return to this later.

## Next Up: Blockciphers

Blockciphers are a ubiquitous crypto tool applied to many different problems.

**Informal definition:** A blockcipher is essentially a substitution cipher with a very large alphabet and a very compact key. Require that efficient algorithms for forward and backward directions.

Typical parameters:

Alphabet =  $\{0,1\}^{128}$

Key length = 16 bytes.

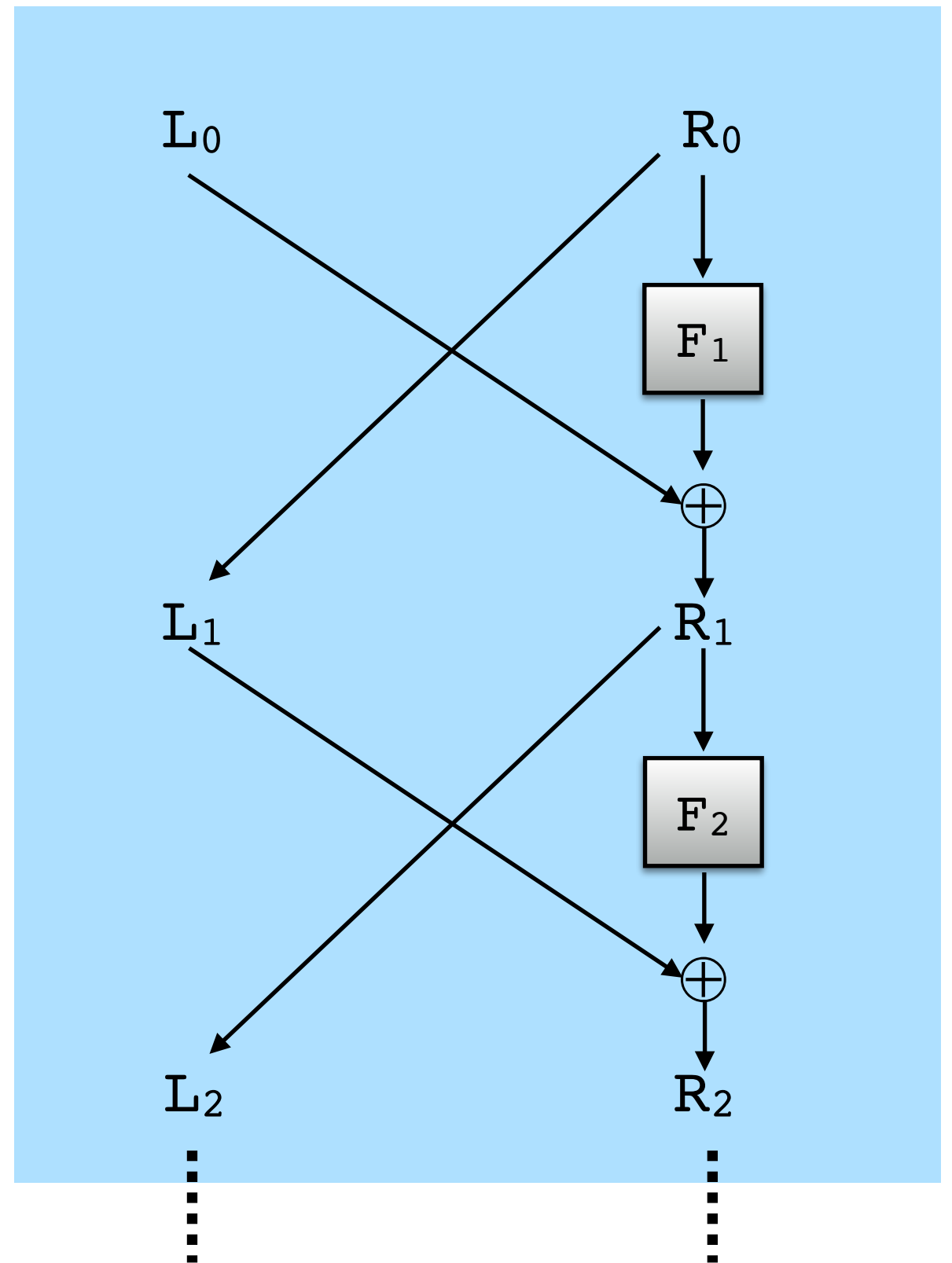
Plan: Build many higher-level protocols from a good blockcipher.

Now: Two example blockciphers, DES and AES.

# Data Encryption Standard (DES)

- Originally designed by IBM
- Parameters adjusted by NSA
- NIST Standard in 1976
  - Block length  $n = 64$
  - Key length  $k = 56$

Parses input block into 32-bit chunks and applies 16 rounds of a “Feistel Network”



# DES is Broken



**Warning: Broken**



Attack	Complexity	Year
Biham&Shamir	$2^{47}$ encrypted blocks	1992
DESCALL	41 days	1997
EFF Deepcrack	4.5 days	1998
EFF Deepcrack	22 hours	1999

- 3DES (“Triple DES”) is still used by banks
- 3DES encrypts three times (so key length is 118)
- 3DES is not known to be broken but should be avoided





# GET CRACKING

These are the types of DES cracking jobs that we support:

[Windows LM/NTLMv1 Authentication](#)

[PPTP VPNs](#) [WPA-Enterprise](#)

[des\\_crypt\(\) Hashes](#)

[DES Kerberos5](#) [Known Plaintext DES](#)

NOTE: There are currently extremely high wait times.  
We're in the process of adding capacity to speed things up.

**QUEUE WAIT TIME:**

**Standard 46.2 Days, ASAP 1.0 Days**

## SUBMIT A JOB!

Token:

Priority:

Enter Token For Pricing ⬆

PAY WITH CARD

**WARNING:** Charges will show up on your credit card statement as from "crack.sh" and processed through Stripe. We've experienced a high number of our charges being reported as fraudulent, so we'll be blacklisting any accounts that contest charges for jobs submitted. If you wish to cancel a job or have any issues, please email [david@toorcon.org](mailto:david@toorcon.org) and we'll be happy to cancel and refund any charges.

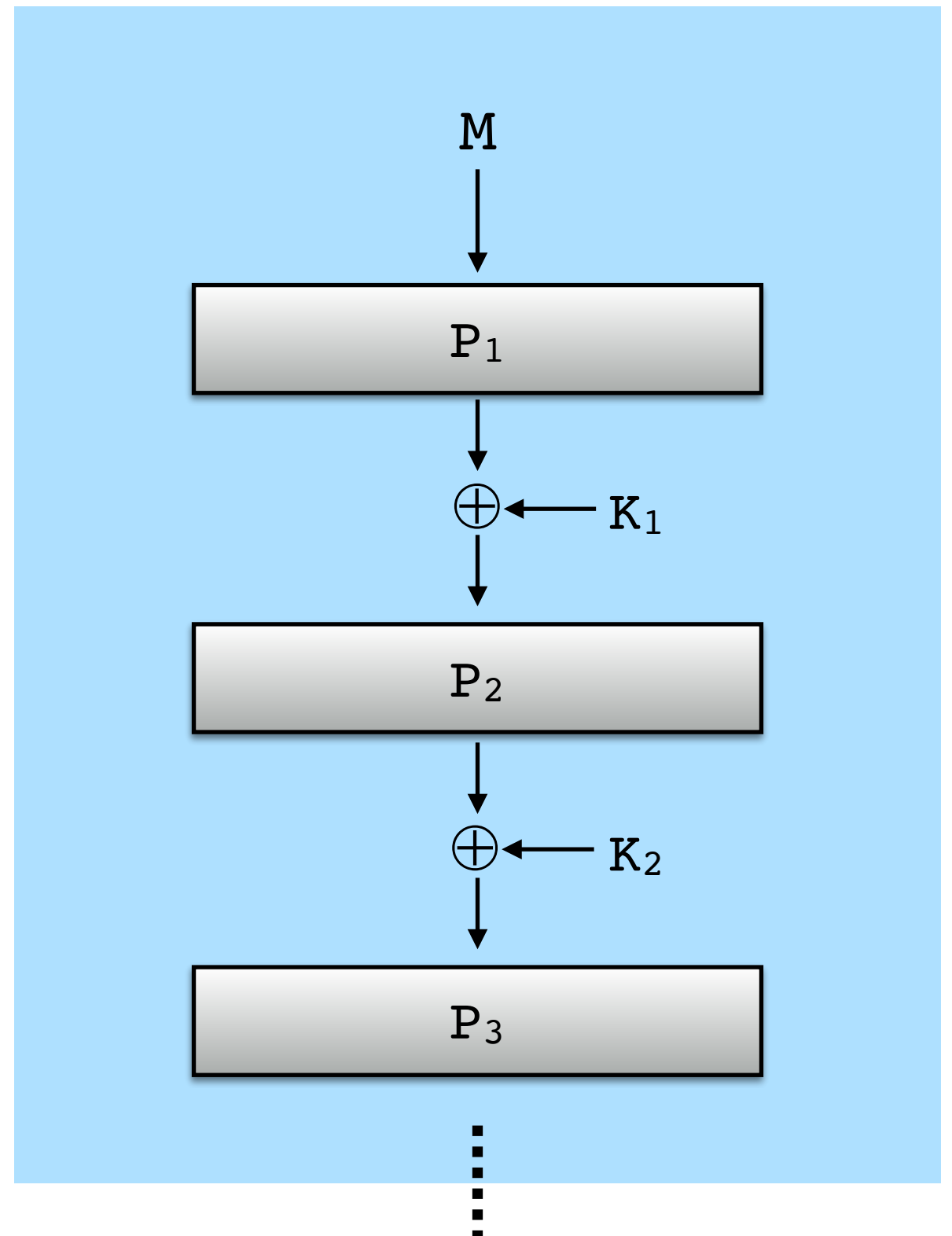
# Advanced Encryption Standard (AES)

- NIST ran competition to replace DES starting in 1997
- Several submissions, *Rijndael* chosen and standardized
- AES is now the gold standard blockcipher
- Very fast; Intel chips even have AES instructions

# Advanced Encryption Standard (AES)

- Due to Rijmen and Daemen
  - Block length  $n = 128$
  - Key length  $k = 128, 192, 256$

- Different structure from DES.
- 10 rounds of “substitution-permutation network”



# AES is not (known to be) broken

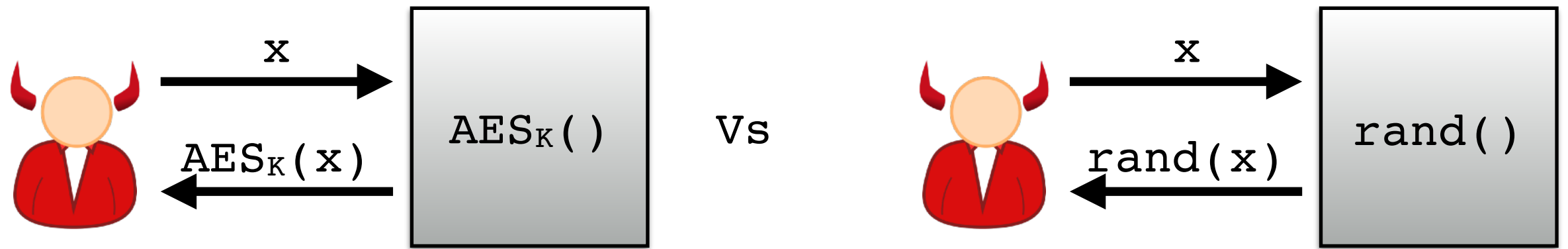
Attack	Complexity	Year
Bogdanov et al.	$\approx 2^{126.1}$	2011

- Compare to trying all keys:  $2^{126.1} \approx 2^{128} / 4$
- Always prefer AES for a blockcipher if setting can support it (i.e. everything except low-power hardware)



# Blockcipher Security

- AES is thought to be a good “Pseudorandom Permutation”



- Outputs all look random and independent, even when inputs are maliciously controlled.
- Formal definition in CS284.

# Example - AES Input/Outputs

- Keys and inputs are 16 bytes = 128 bits

- K1: 9500924ad9d1b7a28391887d95fcfbd5

- K2: 9500924ad9d1b7a28391887d95fcfbd6

$\text{AES}_{K1}(00 \dots 00) = 8b805ddb39f3eee72b43bf95c9ce410f$

$\text{AES}_{K1}(00 \dots 01) = 9918e60f2a20b1b81674646dceebdb51$

$\text{AES}_{K2}(00 \dots 00) = 1303270be48ce8b8dd8316fdbba38eb04$

$\text{AES}_{K2}(00 \dots 01) = 96ba598a55873ec1286af646073e36f6$

# So we have a blockcipher...

- Now what?

It only processes 16 bytes at a time, and I have a whole lot more data than that.

This next step is where everything flies off the rails in implementations...

# Encrypting large files: ECB



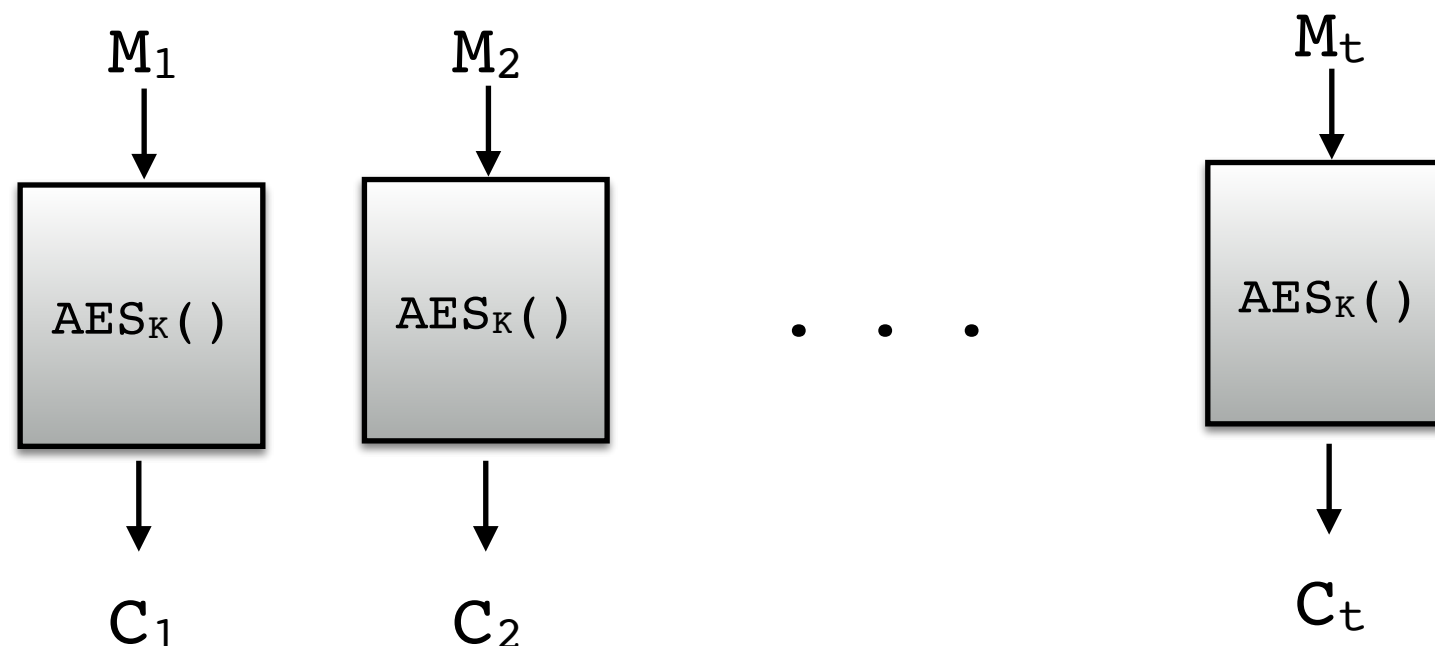
**Warning: Broken**



- ECB = “Electronic Code Book”

## AES-ECB<sub>k</sub>(M)

- Parse M into blocks  $M_1, M_2, \dots, M_t$   
*// all blocks except  $M_t$  are 16 bytes*
- Pad  $M_t$  up to 16 bytes
- For  $i=1\dots t$ :
  - $C_i \leftarrow \text{AES}_k(M_i)$
- Return  $C_1, \dots, C_t$



# The ECB Penguin



**Warning: Broken**

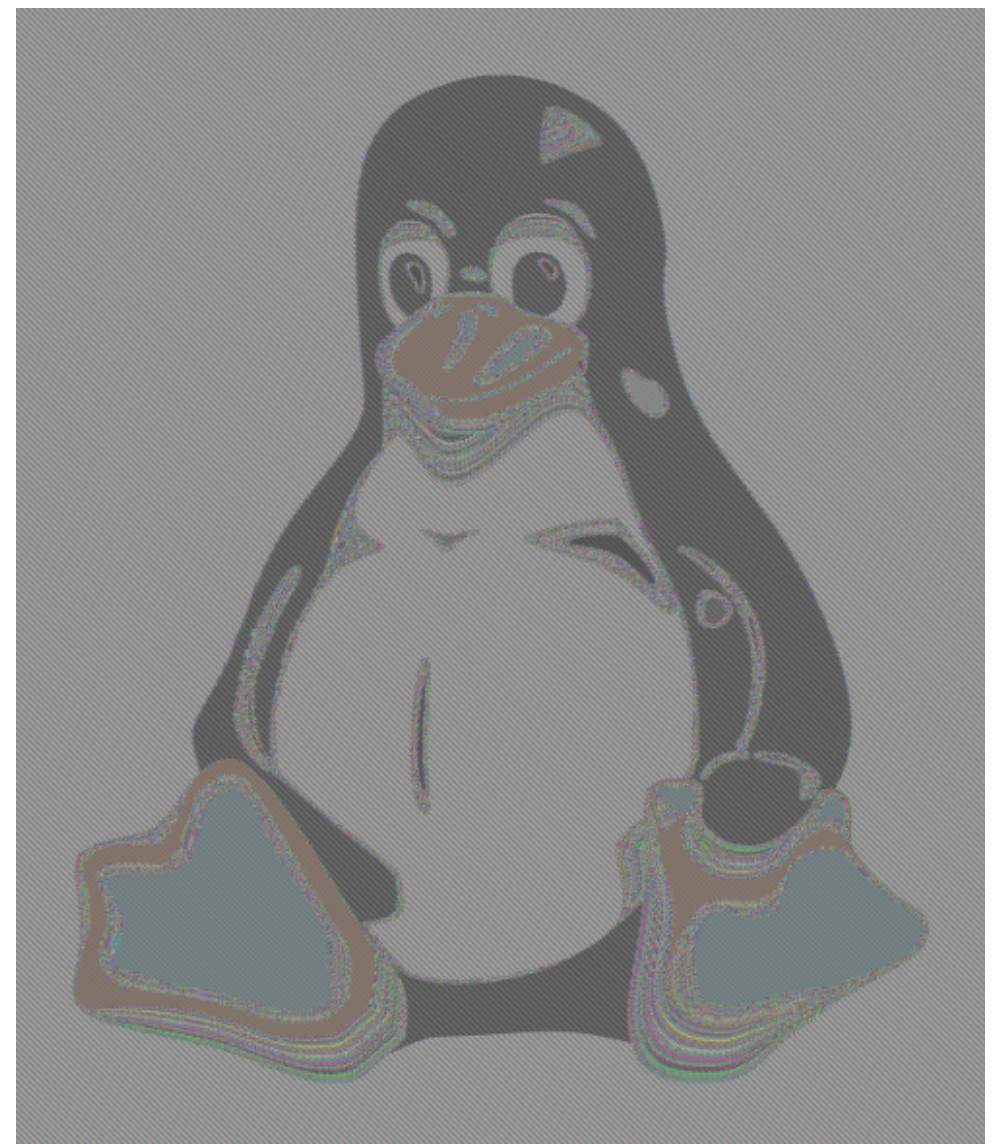


- 16 byte chunks are consecutive pixels

Plaintext



ECB Ciphertext



- It gets even worse...

# Encrypting large files, Attempt #2: CTR

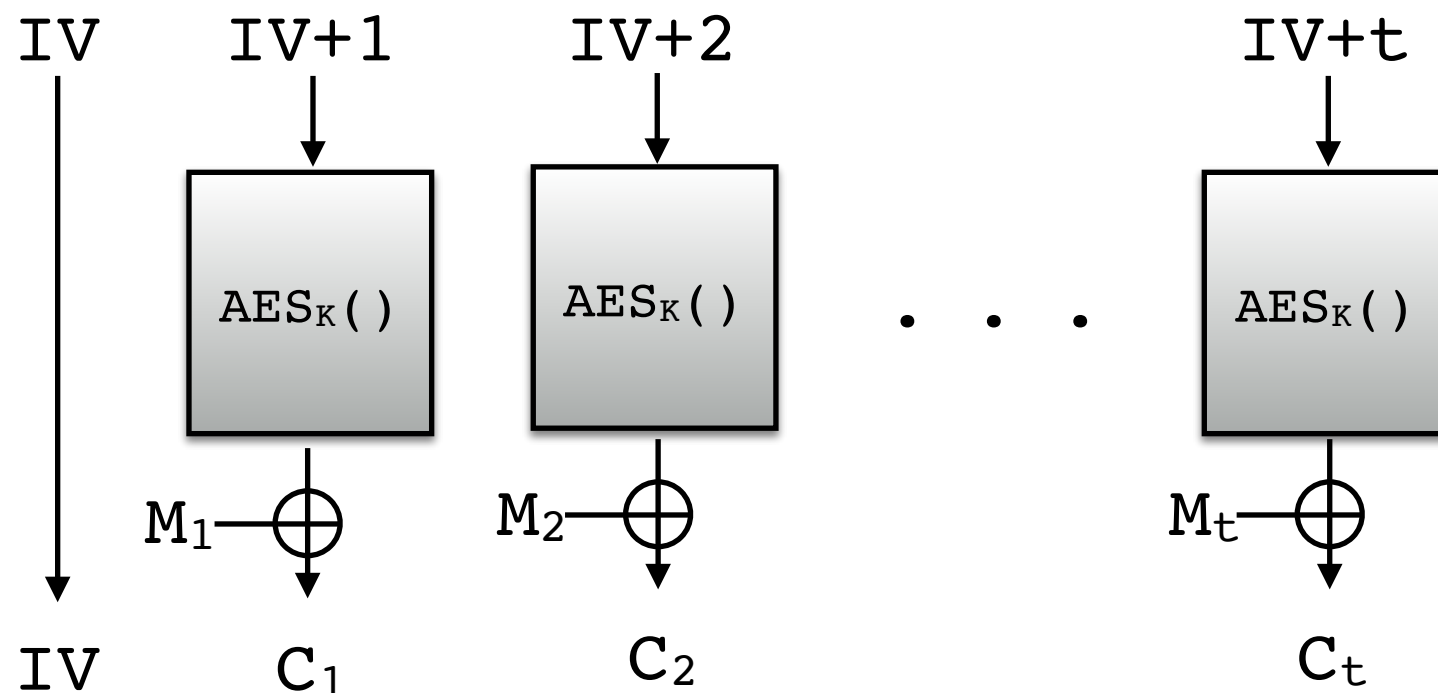
- CTR = “Counter Mode”
- Idea: Build a nonce-based stream cipher from AES

## AES-CTR<sub>k</sub>(IV, M)

- Parse M into blocks  $M_1, M_2, \dots, M_t$   
*// all blocks except  $M_t$  are 16 bytes*
- For  $i=1\dots t$ :
  - $C_i \leftarrow M_i \oplus \text{AES}_k(\text{IV}+i)$
- Return  $\text{IV}, C_1, \dots, C_t$

## Notes:

- No need to pad last block
- Must avoid reusing part of stream



When combined with authentication, CTR is a good cipher.





# Penguin Sanity Check

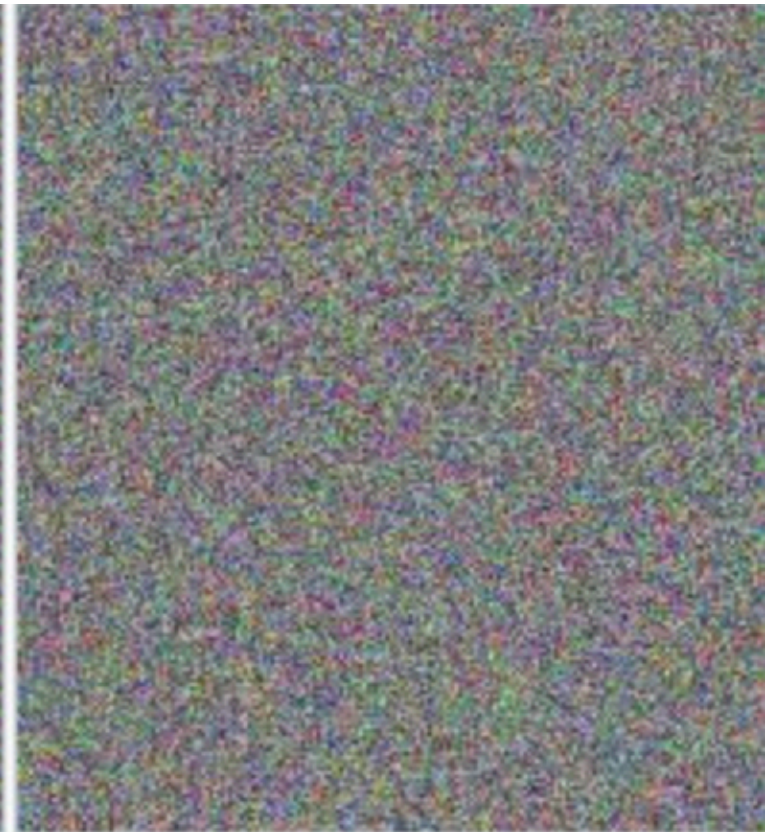
Plaintext



ECB Ciphertext



CTR Ciphertext



Looks random

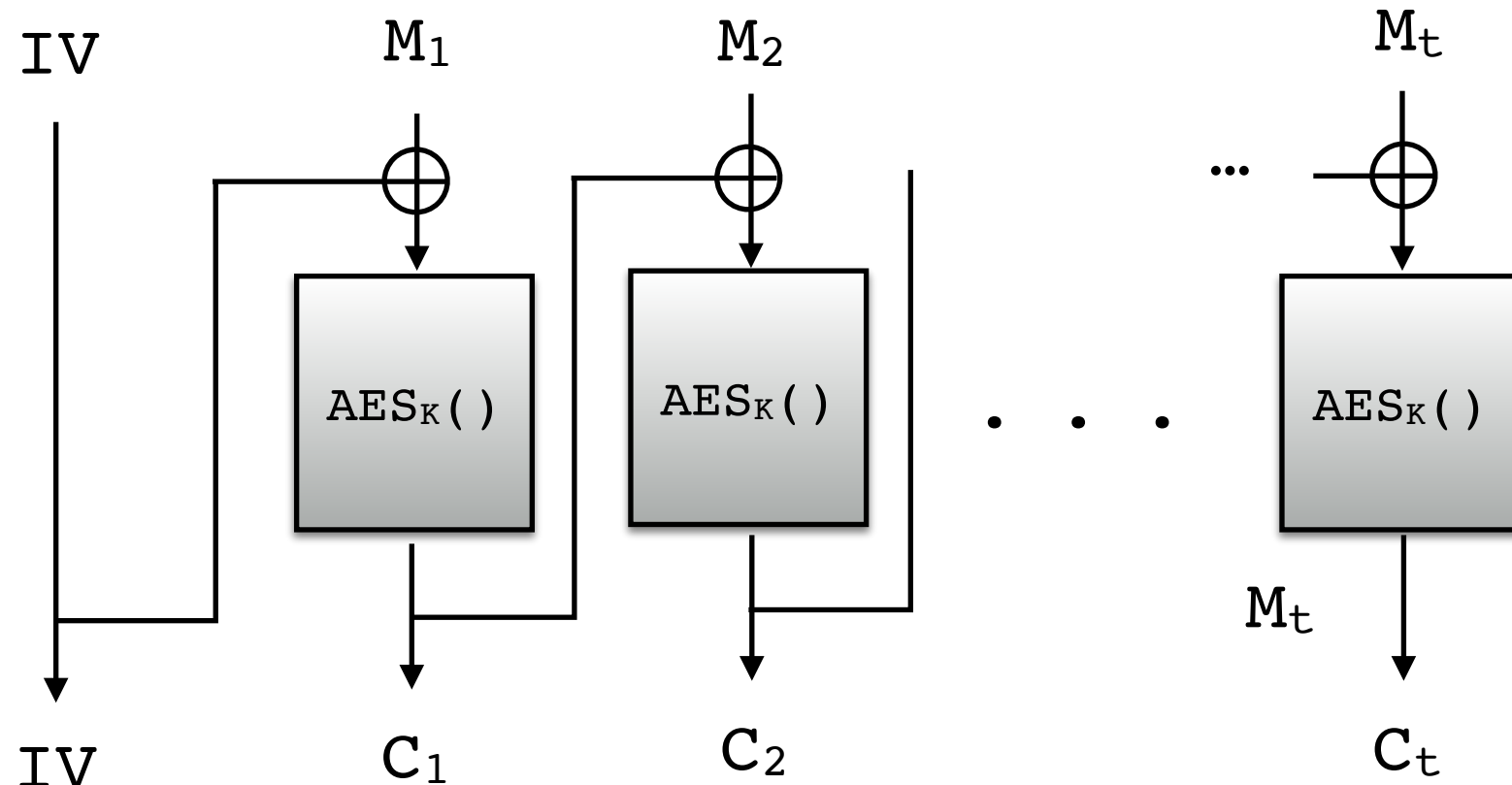


# Encrypting large files, Attempt #3: CBC

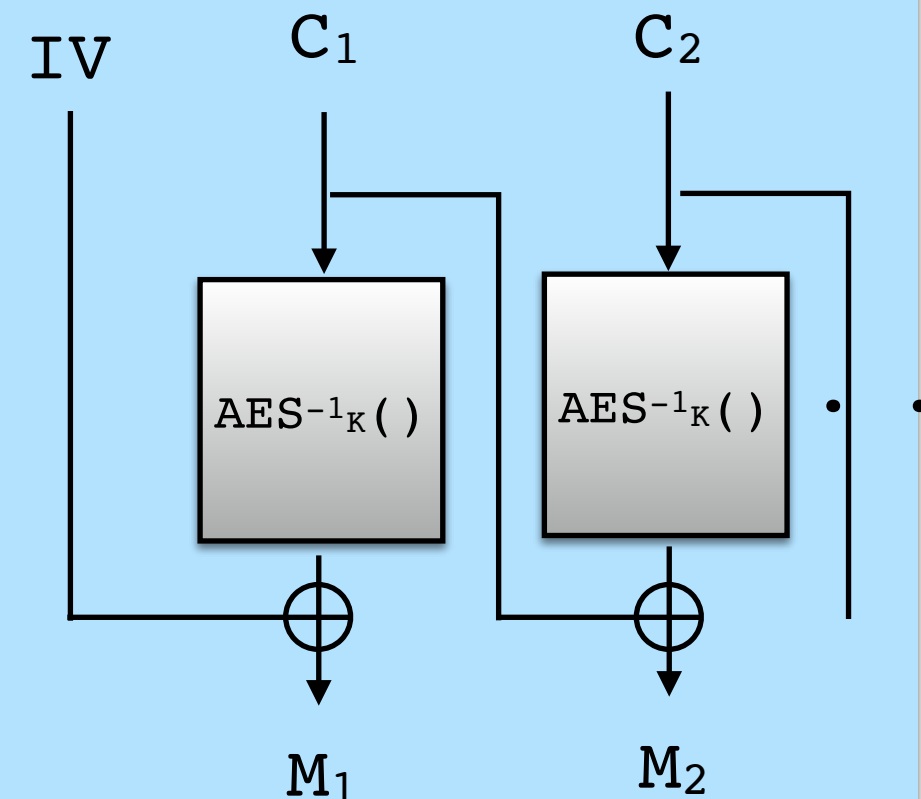
- CBC = “Cipher Block Chaining”
- Nonce-based, but not a stream cipher
- Historical option (sometimes used without nonce)

## AES-CBC<sub>k</sub>(IV, M)

- Parse M into blocks  $M_1, M_2, \dots, M_t$   
// all blocks except  $M_t$  are 16 bytes
- Pad  $M_t$  up to 16 bytes
- $C_0 \leftarrow IV$
- For  $i=1..t$ :
  - $C_i \leftarrow \text{AES}_k(M_i \oplus C_{i-1})$
- Return  $C_0, C_1, \dots, C_t$



## Decryption



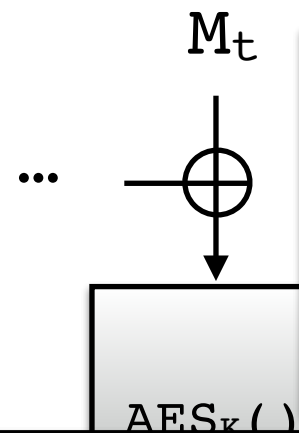
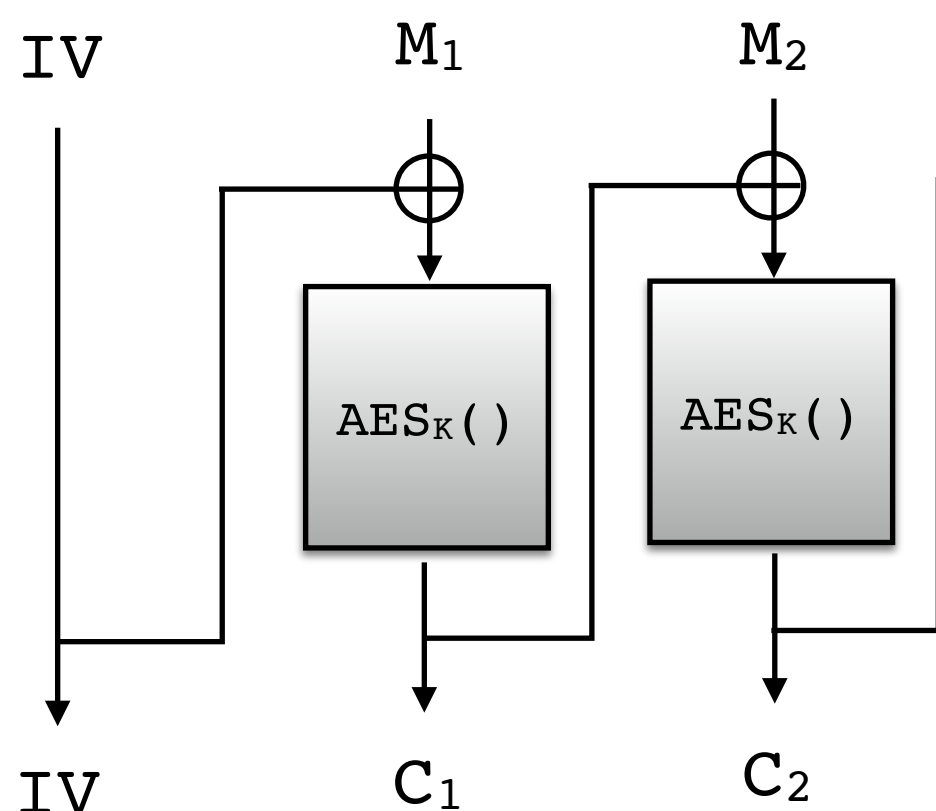


# Encrypting large files, Attempt #3: CBC

- CBC = “Cipher Block Chaining”
- Nonce-based, but not a stream cipher
- Historical option (sometimes used without nonce)

## AES-CBC<sub>k</sub>(IV, M)

- Parse M into blocks  $M_1, M_2, \dots, M_t$   
// all blocks except  $M_t$  are 16 bytes
- Pad  $M_t$  up to 16 bytes
- $C_0 \leftarrow IV$
- For  $i=1..t$ :
  - $C_i \leftarrow \text{AES}_k(M_i \oplus C_{i-1})$
- Return  $C_0, C_1, \dots, C_t$



When combined with authentication, CBC is a good cipher.



Warning: Padding creates havoc with authentication. Very difficult to implement.

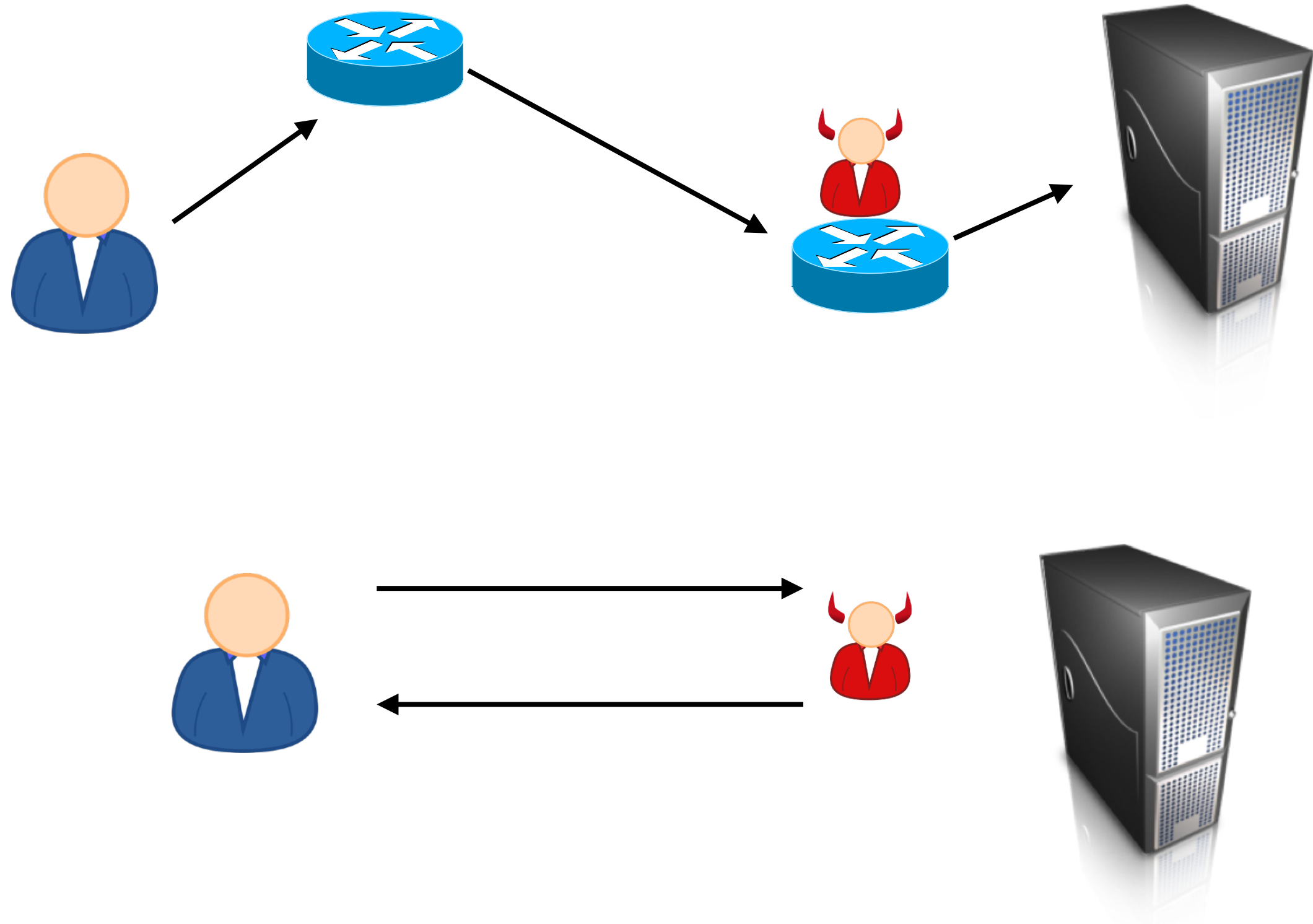
# Blockcipher Encryption Summary

- AES is unbroken
- AES-CTR is most robust construction for confidentiality
- AES-CTR/AES-CBC do not provide authenticity/integrity and should almost never be used alone.

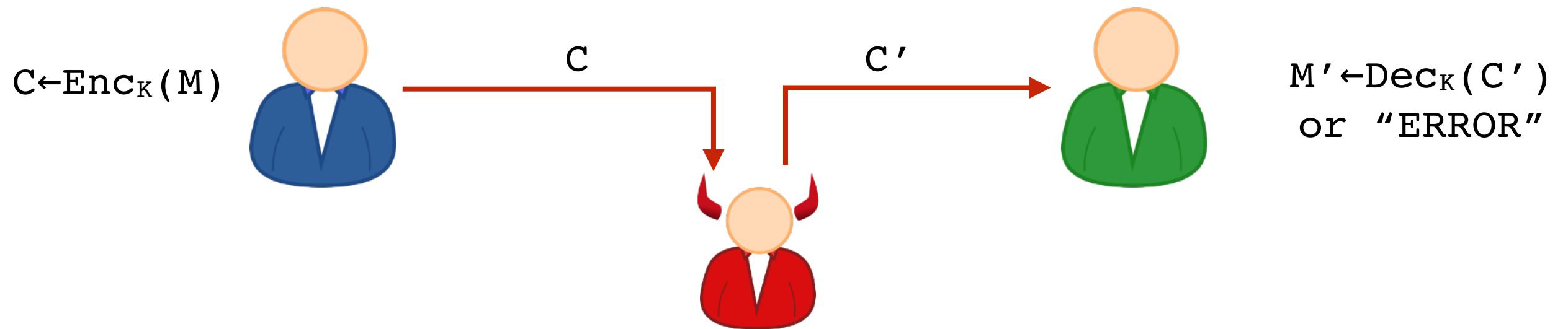
## Next Up: Integrity and Authentication

- Authenticity: Guarantee that adversary cannot change or insert ciphertexts
- Achieved with MAC = “Message Authentication Code”

# Integrity: Preventing message modification



# Encryption Integrity: An abstract setting



Encryption satisfies **integrity** if it is infeasible for an adversary to send a new  $C'$  such that  $\text{Dec}_K(C') \neq \text{ERROR}$ .

# AES-CTR does not satisfy integrity

M = please pay ben 20 bucks

C = b0595fafd05df4a7d8a04ced2d1ec800d2daed851ff509b3e446a782871c2d

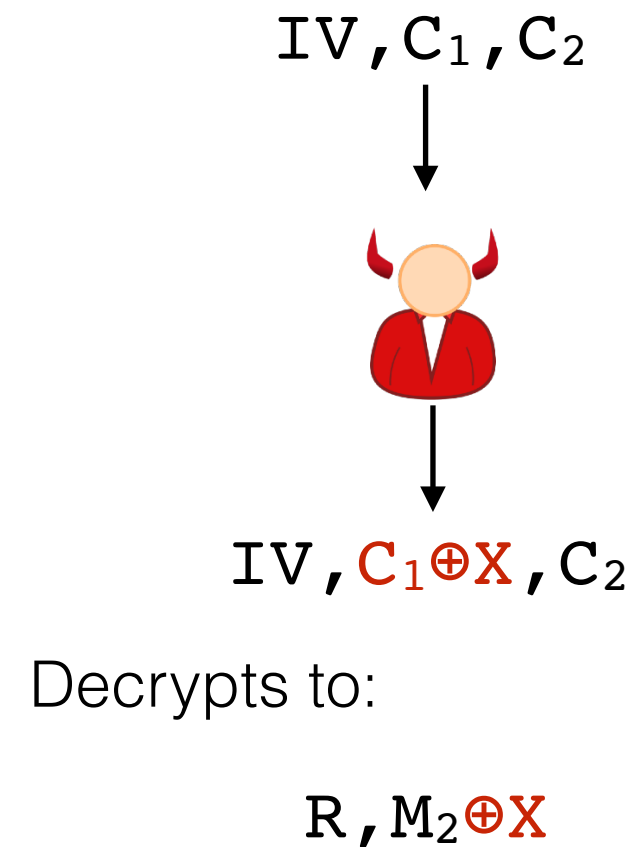
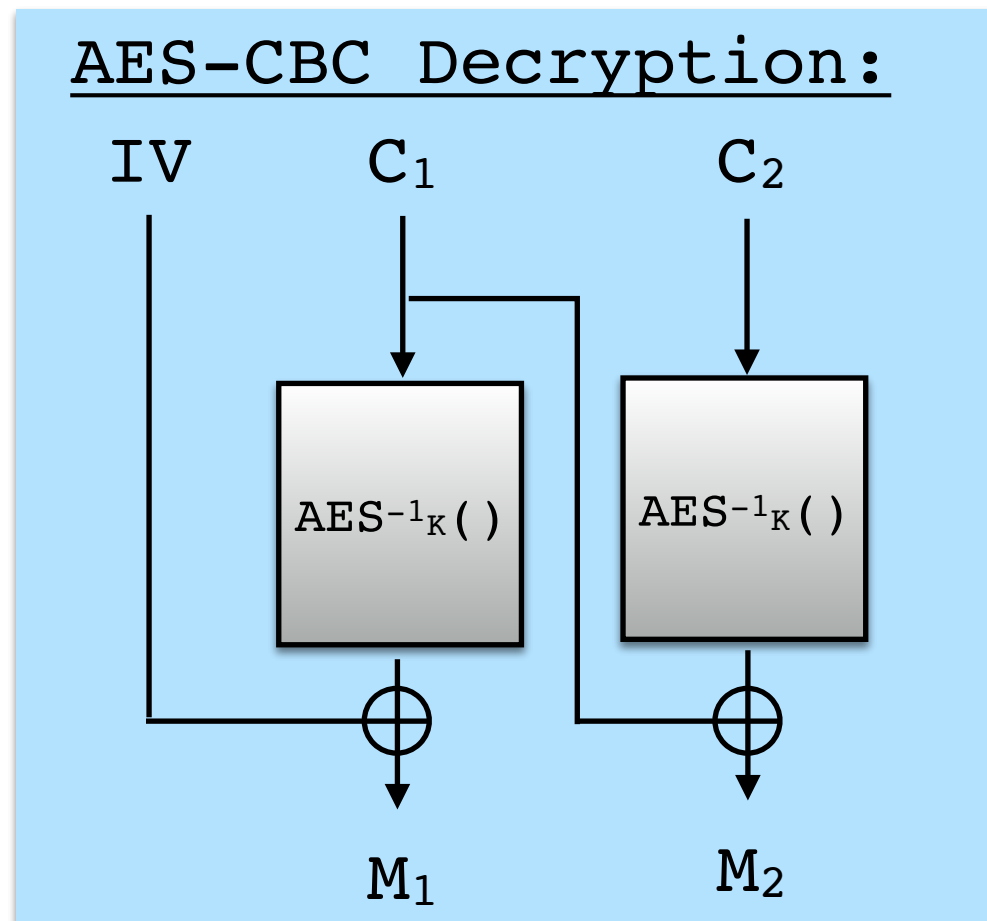


C' = b0595fafd05df4a7d8a04ced2d1ec800d2daed851ff509b3e546a782871c2d

M' = please pay ben 21 bucks

Inherent to stream-cipher approach to encryption.

# AES-CBC does not satisfy integrity



Where  $R$  is some unpredictable block.

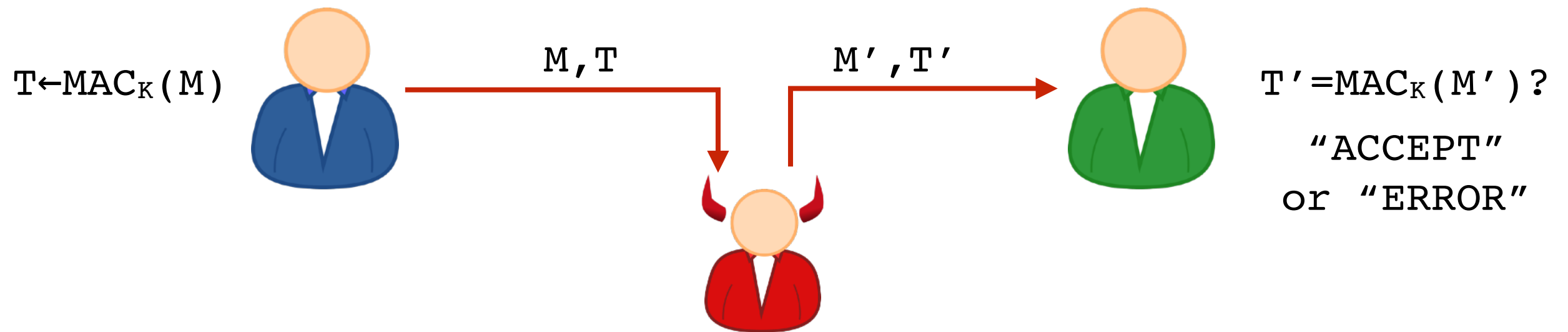
# Message Authentication Code

A **message authentication code (MAC)** is an algorithm that takes as input a key and a message, and outputs an “unpredictable” **tag**.





# MAC Security Goal: Unforgeability



MAC satisfies **unforgeability** if it is unfeasible for Adversary to fool Bob into accepting  $M'$  not previously sent by Alice.

# MAC Security Goal: Unforgeability

*Note: No encryption on this slide.*

$M$  = please pay ben 20 bucks

$T$  = 827851dc9cf0f92ddcdc552572ffd8bc



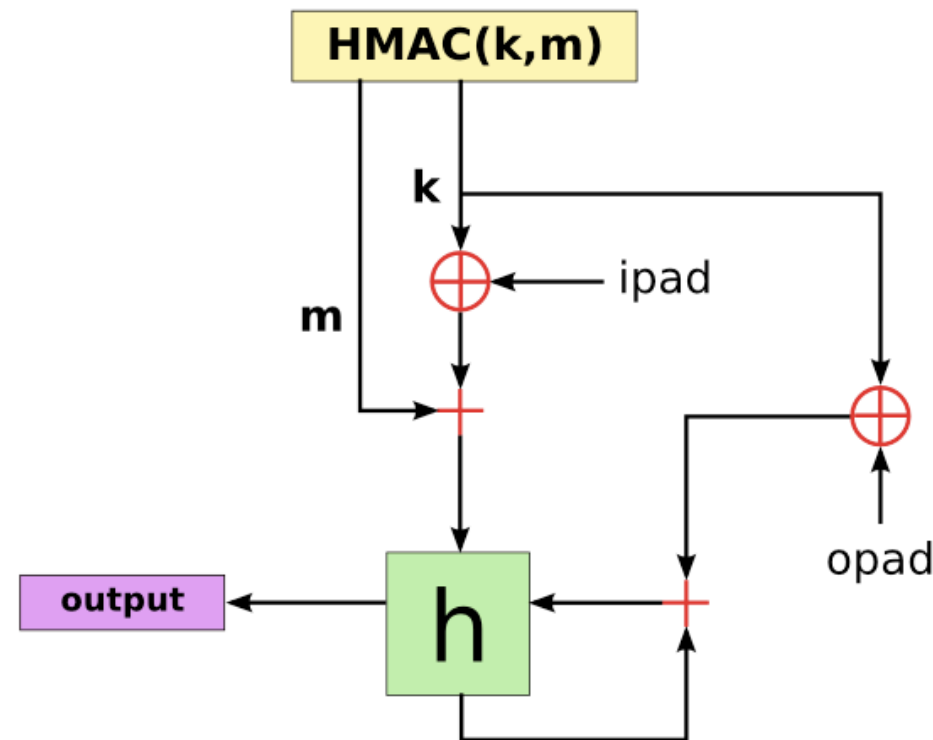
$M'$  = please pay ben 21 bucks

$T'$  = baeaf48a891de588ce588f8535ef58b6

Should be hard to predict  $T'$  for any new  $M'$ .

# MACs In Practice: Pretty much always use HMAC

- Don't worry about how it works.
- More precisely: Use HMAC-SHA2. More on hashes and MACs later.



- Other options: Poly1305-AES or CBC-MAC (the latter is tricky)

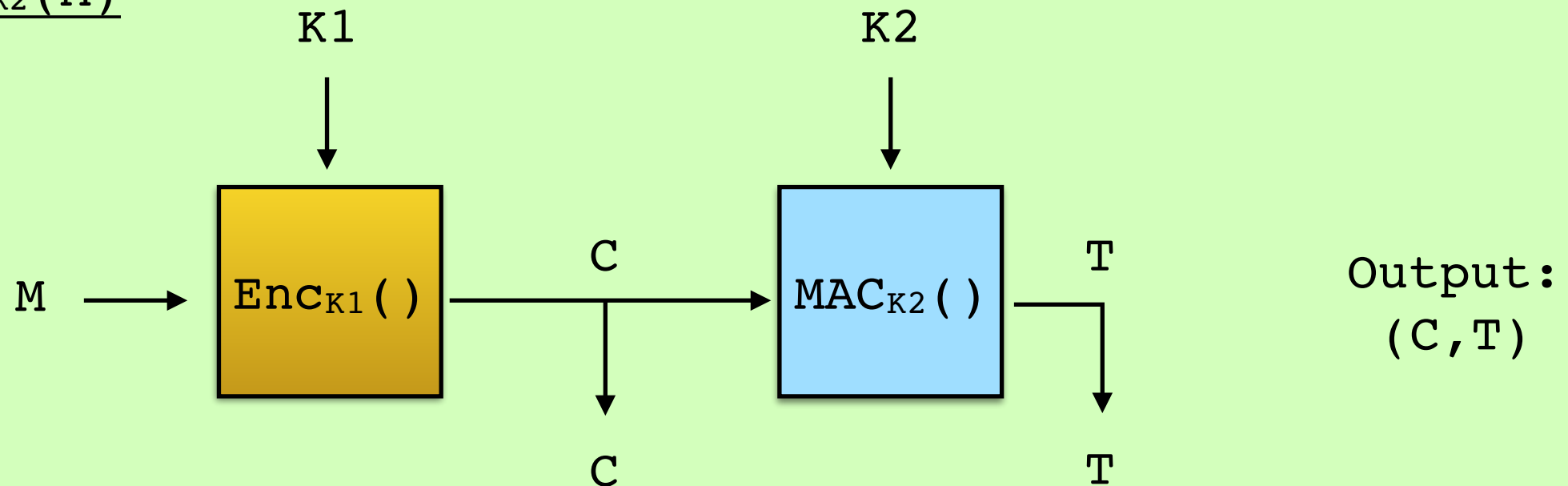
# Authenticated Encryption

Encryption that provides **confidentiality** and **integrity** is called **Authenticated Encryption**.

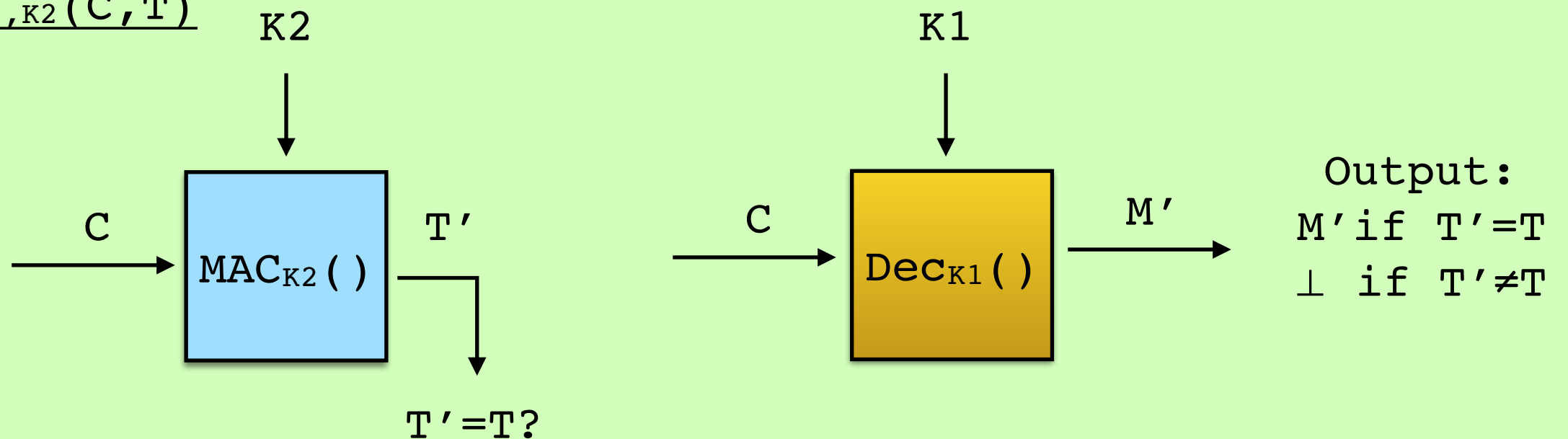
- Built using a good cipher and a MAC.
  - Ex: AES-CTR with HMAC-SHA2
- Best solution: Use ready-made Authenticated Encryption
  - Ex: AES-GCM is the standard

# Building Authenticated Encryption

Encrypt<sub>K1, K2</sub>(M)



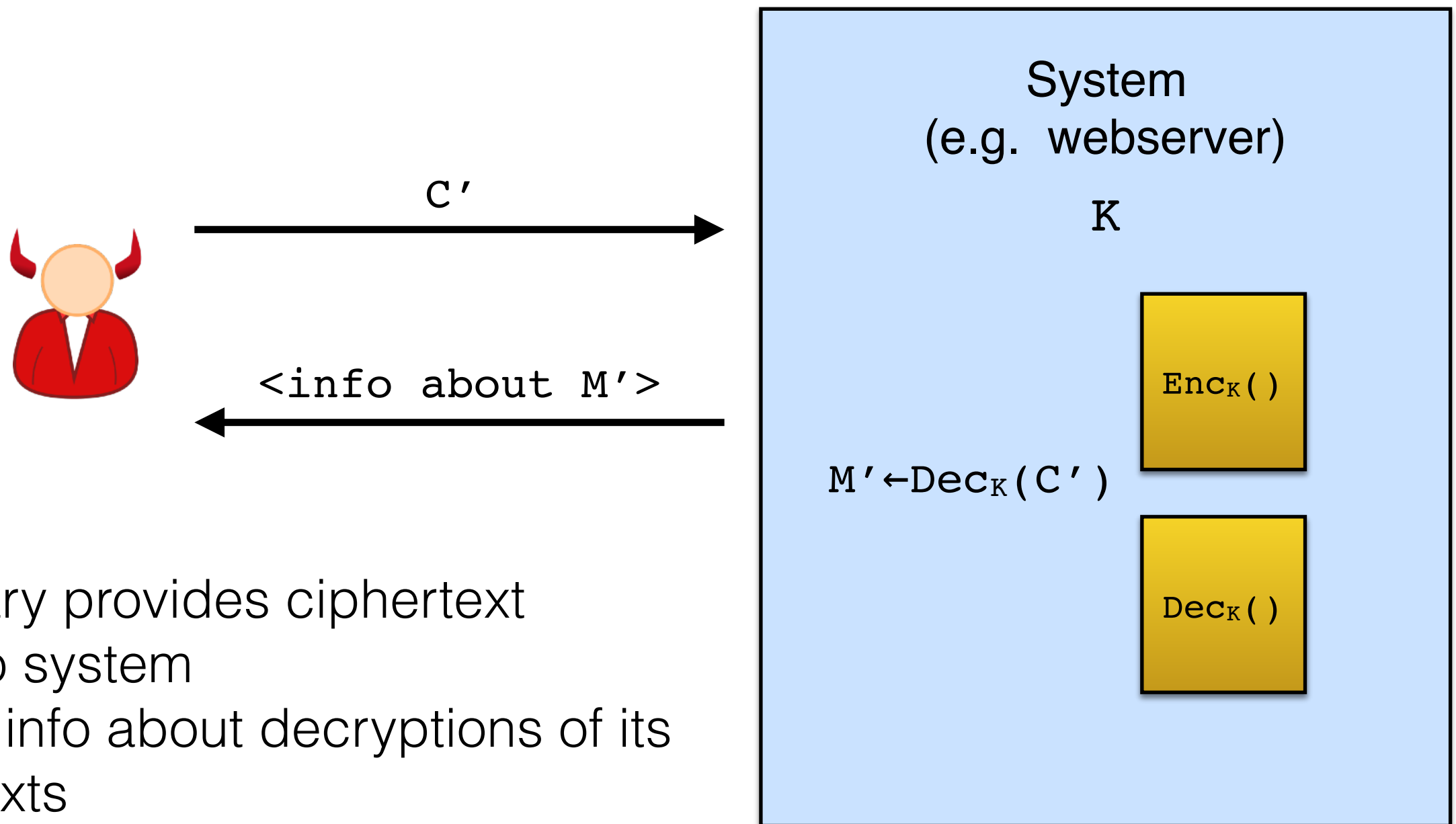
Decrypt<sub>K1, K2</sub>(C, T)



- Summary: MAC the ciphertext, not the message

# Chosen-Ciphertext Attacks (CCA) against Encryption

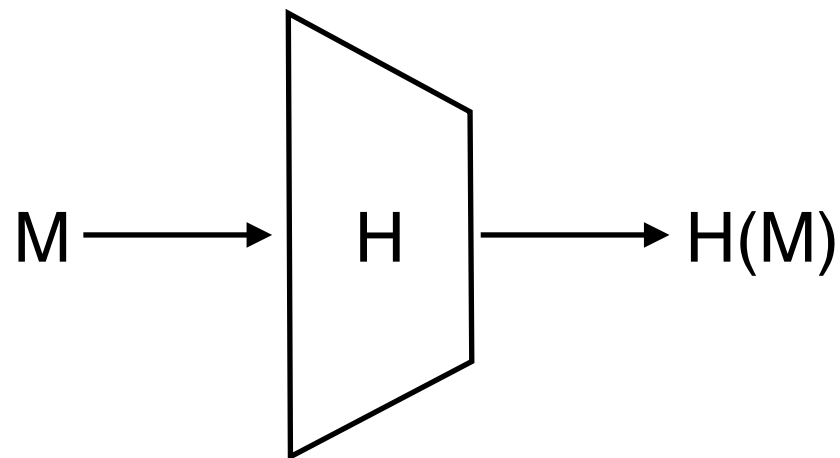
- Integrity + Confidentiality = security against CCAs



- Adversary provides ciphertext inputs to system
- Obtains info about decryptions of its ciphertexts

# Next Up: Hash Functions

**Definition:** A hash function is a deterministic function  $H$  that reduces arbitrary strings to fixed-length outputs.



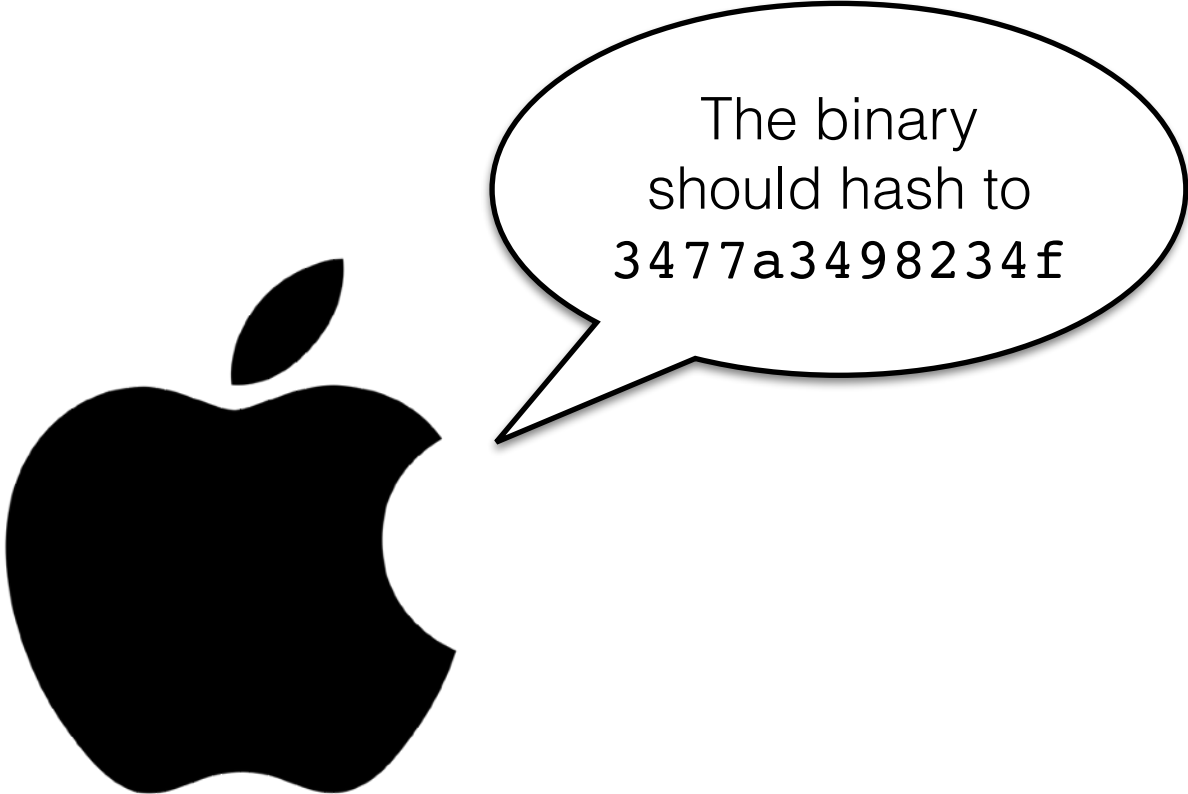
	<u>Output length</u>
MD5:	$m = 128$ bits
SHA-1:	$m = 160$ bits
SHA-256:	$m = 256$ bits
SHA-512:	$m = 512$ bits
SHA-3:	$m \geq 224$ bits


Some security goals:

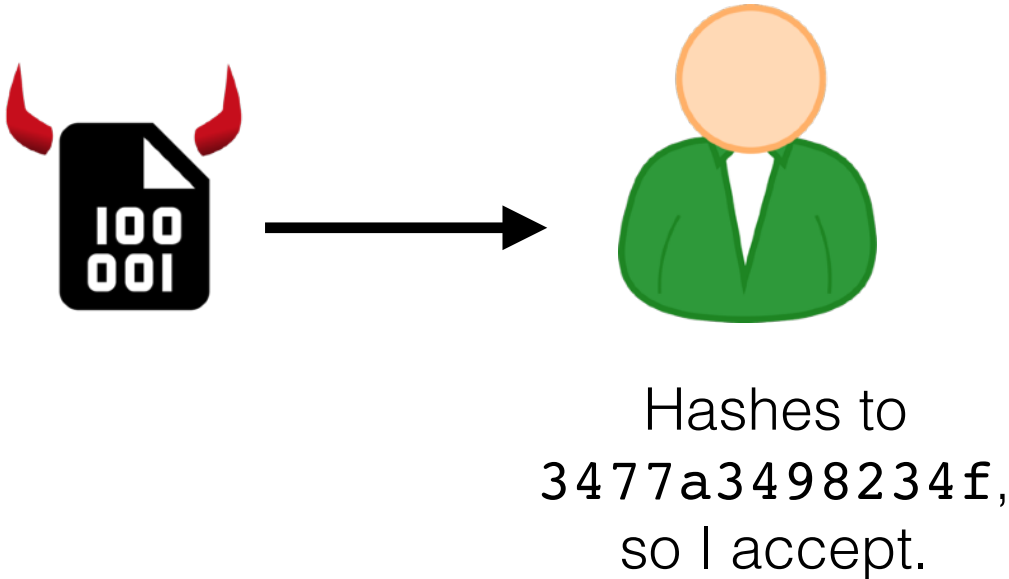
- collision resistance: can't find  $M \neq M'$  such that  $H(M) = H(M')$
- preimage resistance: given  $H(M)$ , can't find  $M$
- second-preimage resistance: given  $H(M)$ , can't find  $M'$  s.t.  
 $H(M') = H(M)$


Note: Very different from hashes used in data structures!


# Why are collisions bad?



MD5 (  ) = 3477a3498234f

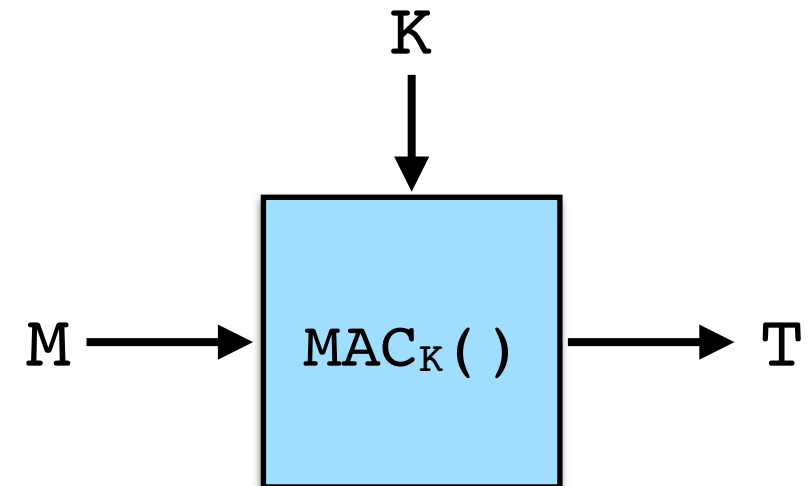
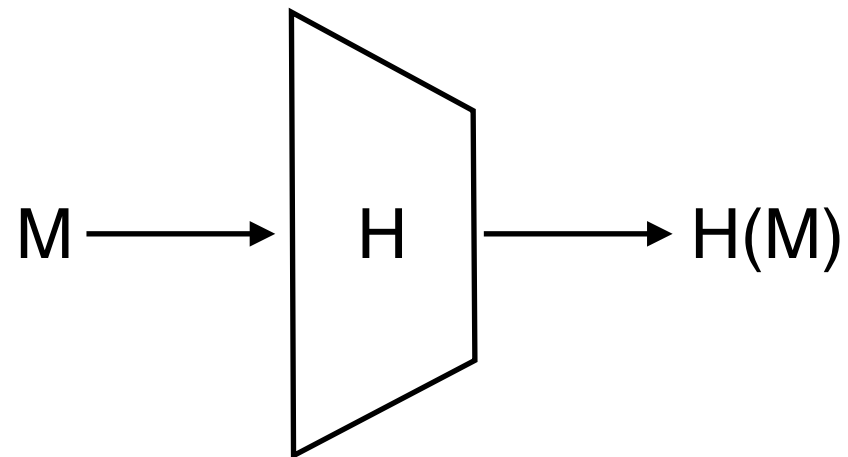




MD5 (  ) = 3477a3498234f



# Hash Functions are not MACs



Both map long inputs to short outputs... But a hash function does not take a key.

**Intuition:** a MAC is like a hash function, that only the holders of key can evaluate.

# Hash Function Security History

- Can always find a collision in  $2^{m/2}$  time ( $\ll 2^m$  time). “Birthday Attack”
- MD5 (1992) was broken in 2004 - can now find collisions very quickly.
- SHA-1 (1995) was broken in 2017 - A big computer can find collisions
- SHA-256/SHA-512 (2001) are not broken
- SHA-3 (2015) is new and not broken

MD5(

d131dd02c5e6eec4693d9a0698aff95c 2fcab58712467eab4004583eb8fb7f89  
55ad340609f4b30283e488832571415a 085125e8f7cdc99fd91dbdf280373c5b )  
d8823e3156348f5bae6dacd436c919c6 dd53e2b487da03fd02396306d248cda0  
e99f33420f577ee8ce54b67080a80d1e c69821bcb6a8839396f9652b6ff72a70

= MD5(

d131dd02c5e6eec4693d9a0698aff95c 2fcab50712467eab4004583eb8fb7f89  
55ad340609f4b30283e4888325f1415a 085125e8f7cdc99fd91dbd7280373c5b )  
d8823e3156348f5bae6dacd436c919c6 dd53e23487da03fd02396306d248cda0  
e99f33420f577ee8ce54b67080280d1e c69821bcb6a8839396f965ab6ff72a70



Xiaoyun Wang (Tsinghua University), 2004

- Broken with clever techniques
- Compare to DES (broken b/c key too short)

**In Assignment 2:** Install and use actual attack code to see how MD5 can be abused.

# MACs from Hash Functions

**Goal:** Build a secure MAC out of a good hash function.

In Assignment 2: Break this construction!

Construction:  $\text{MAC}(K, M) = H(K \parallel M)$



**Warning: Broken**



- Totally insecure if  $H = \text{MD5, SHA1, SHA-256, SHA-512}$
- Is secure with SHA-3

Construction:  $\text{MAC}(K, M) = H(M \parallel K)$



**Just don't**



Upshot: Use HMAC; It's designed to avoid this and other issues.

Later: Hash functions and certificates

The End