

This homework assignment is a written assignment about parsing and typechecking. Please turn in your completed homework at the **beginning** of class on Tuesday, November 22.

1. Consider the following augmented grammar G of expressions.

$$\begin{aligned} S' &\rightarrow E \\ E &\rightarrow \text{id} \\ E &\rightarrow \text{id} (E) \\ E &\rightarrow E * \text{id} \end{aligned}$$

- (a) Calculate First and Follow for G .
 - (b) Build the LR(0) DFA (*i.e.*, states and goto edges) for the grammar. Your answer should clearly define the set of LR(0) items for each state and include a diagram of the DFA.
 - (c) Give the LR(0) action and goto tables for the grammar (remember that the goto table is different from the goto edges!). Is this grammar LR(0)? If not, why?
 - (d) Is this grammar SLR? If not, why?
 - (e) Is this grammar LR(1)? If not, why?
2. Recall the discussion in Handout 4 (*Basic Polymorphic Typechecking*). Assume that we have both `int` and `real` as base types. To extend the typechecker to support overloaded functions (*e.g.*, “+”) on integers and reals, we need to allow type variables that are restricted to be members of some set. For example, the type of “+” could be written as

$$\forall \alpha \in \{\text{int}, \text{real}\}. (\alpha \times \alpha) \rightarrow \alpha$$

We can model this semantics by changing the representation of type-variable kinds:

```
and tvar_kind
= INSTANCE of ty
| UNIV of int
| NUMKIND
```

Give a modified version of the destructive unification algorithm given in Figure 5 that deals with this new kind representation. The idea is that if a type variable has `NUMKIND` kind, then it can only be unified with other type variables or with numeric base types.