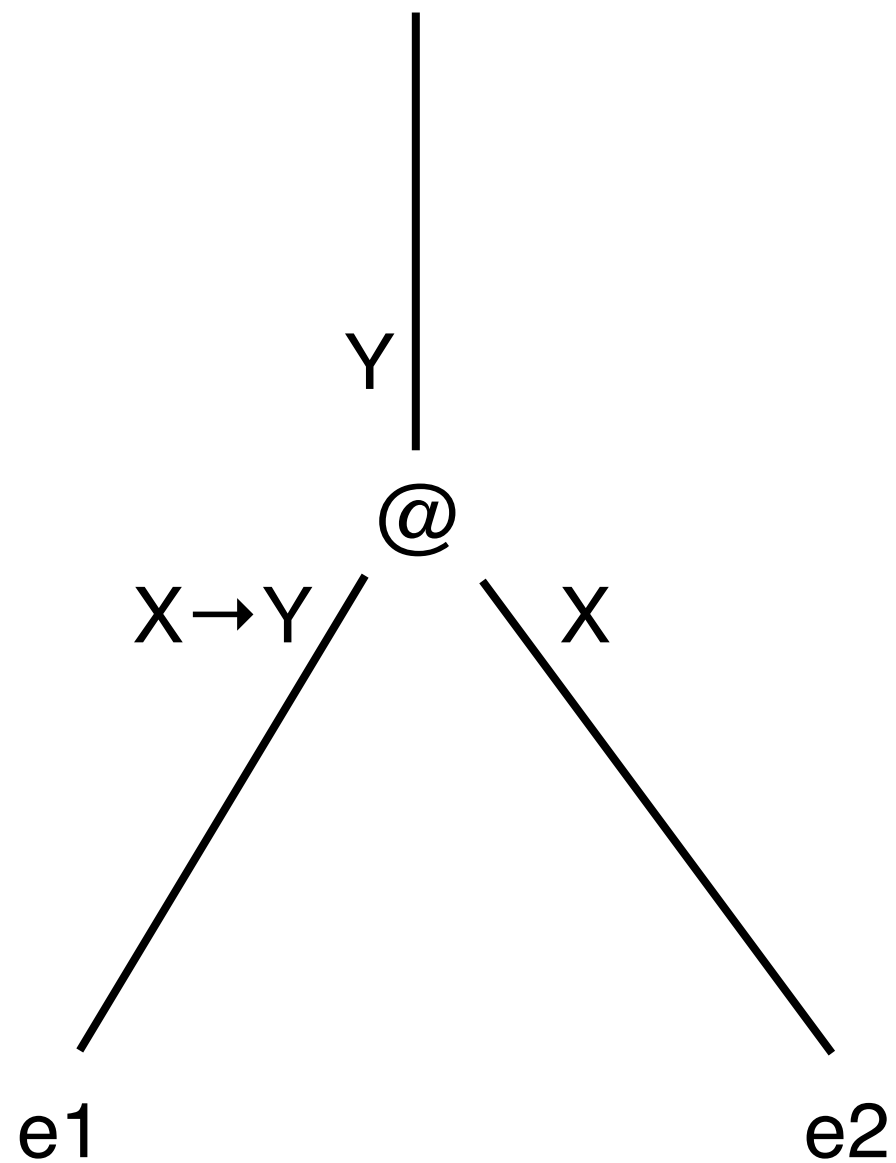
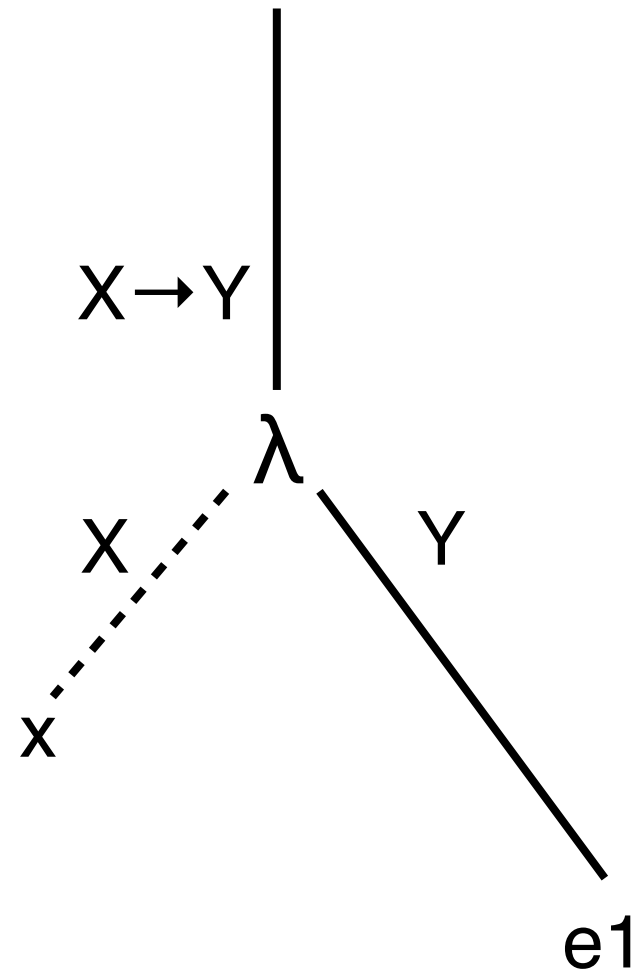


$\vdash e1 : X \rightarrow Y \quad \vdash e2 : X$

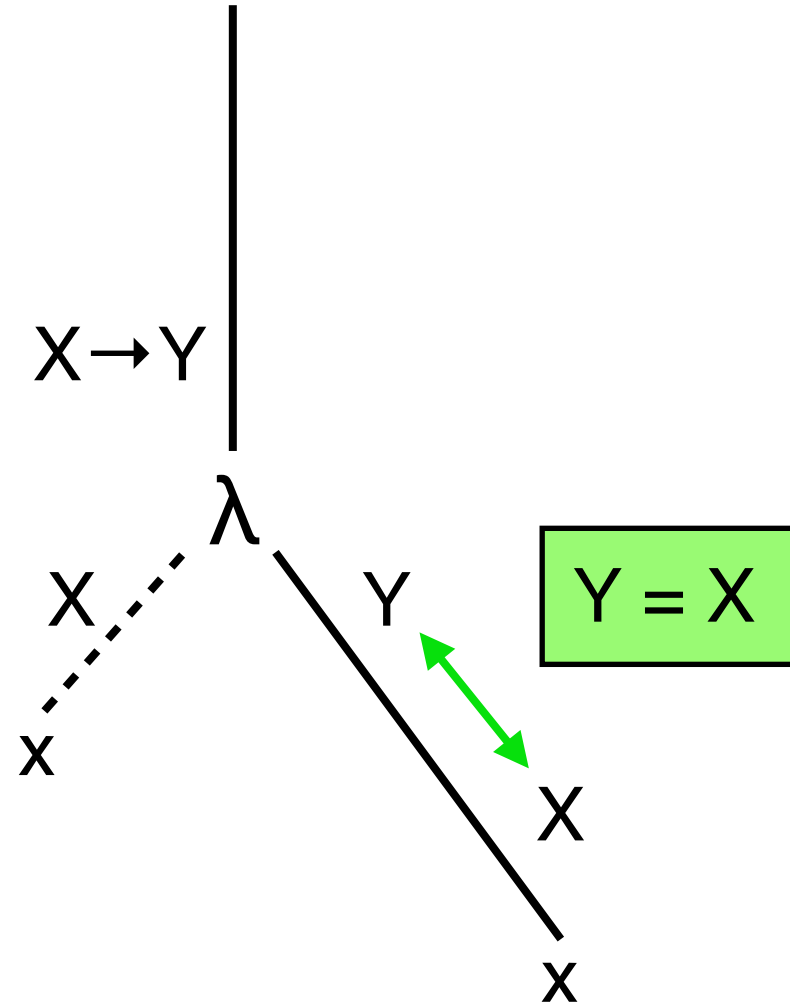
$\vdash e1 @ e2 : Y$



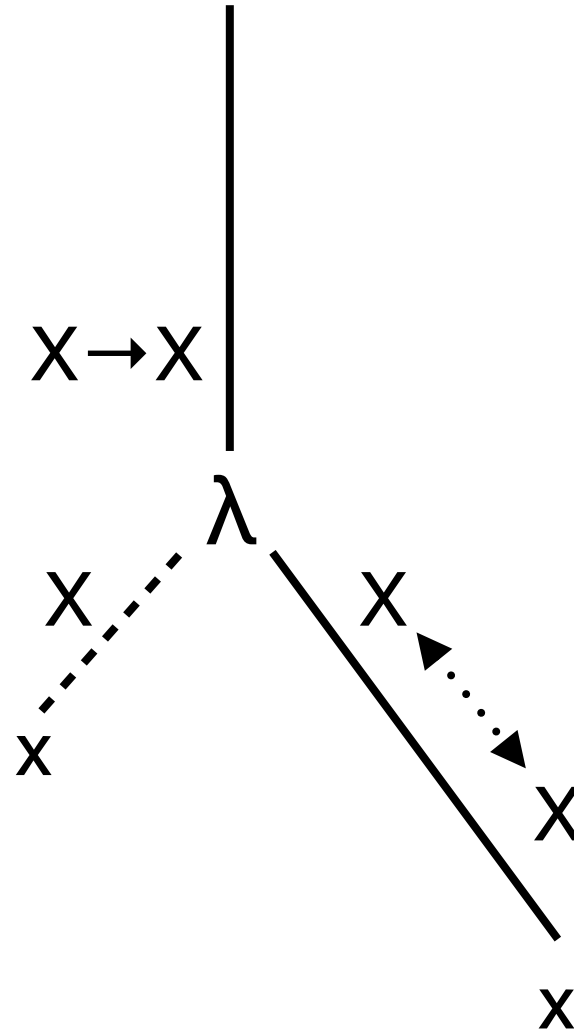
$$x : X \vdash e1 : Y$$

$$\vdash \lambda x. e1 : X \rightarrow Y$$


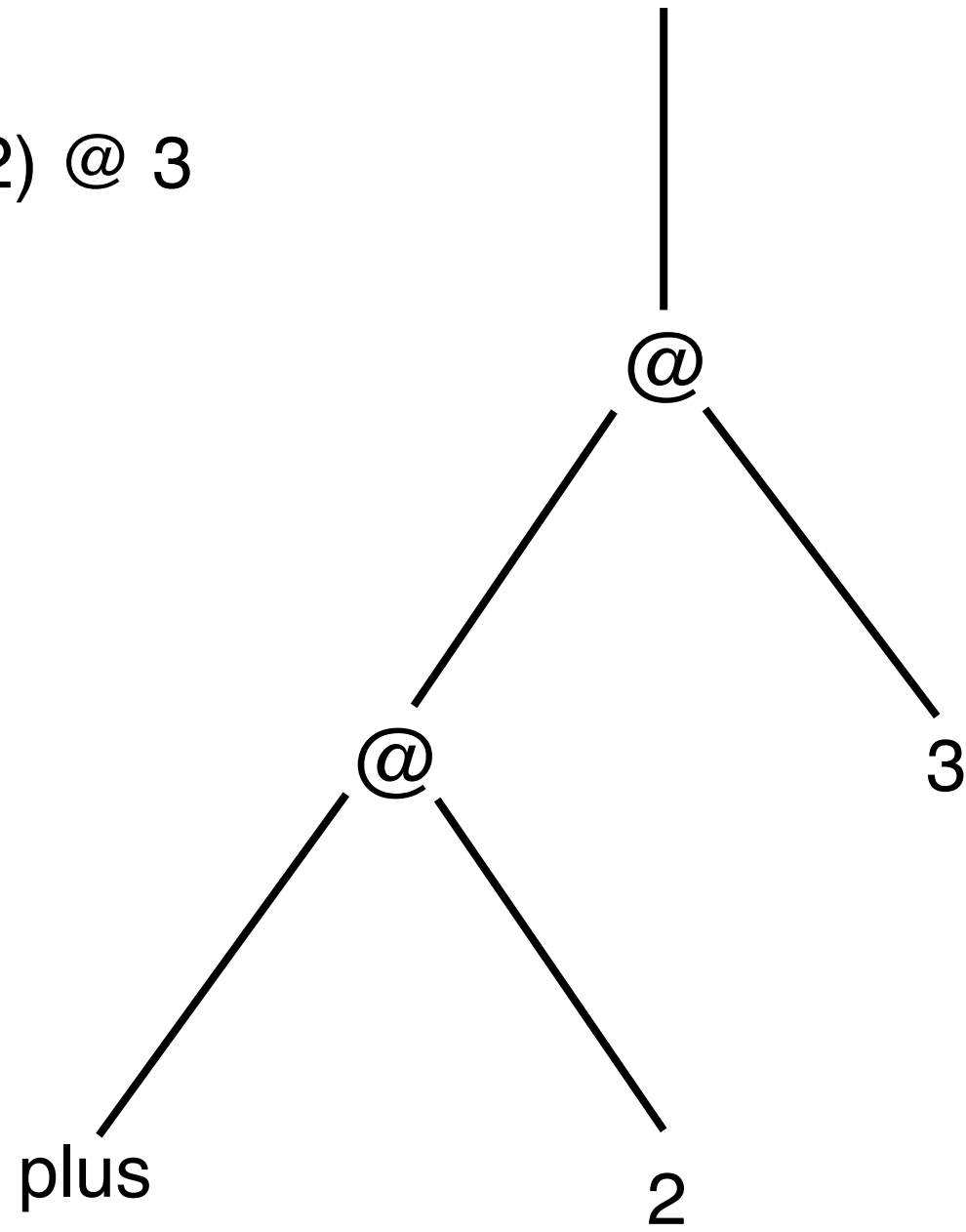
$\vdash \lambda x. x : X \rightarrow X$



$\vdash \lambda x. x : X \rightarrow X$

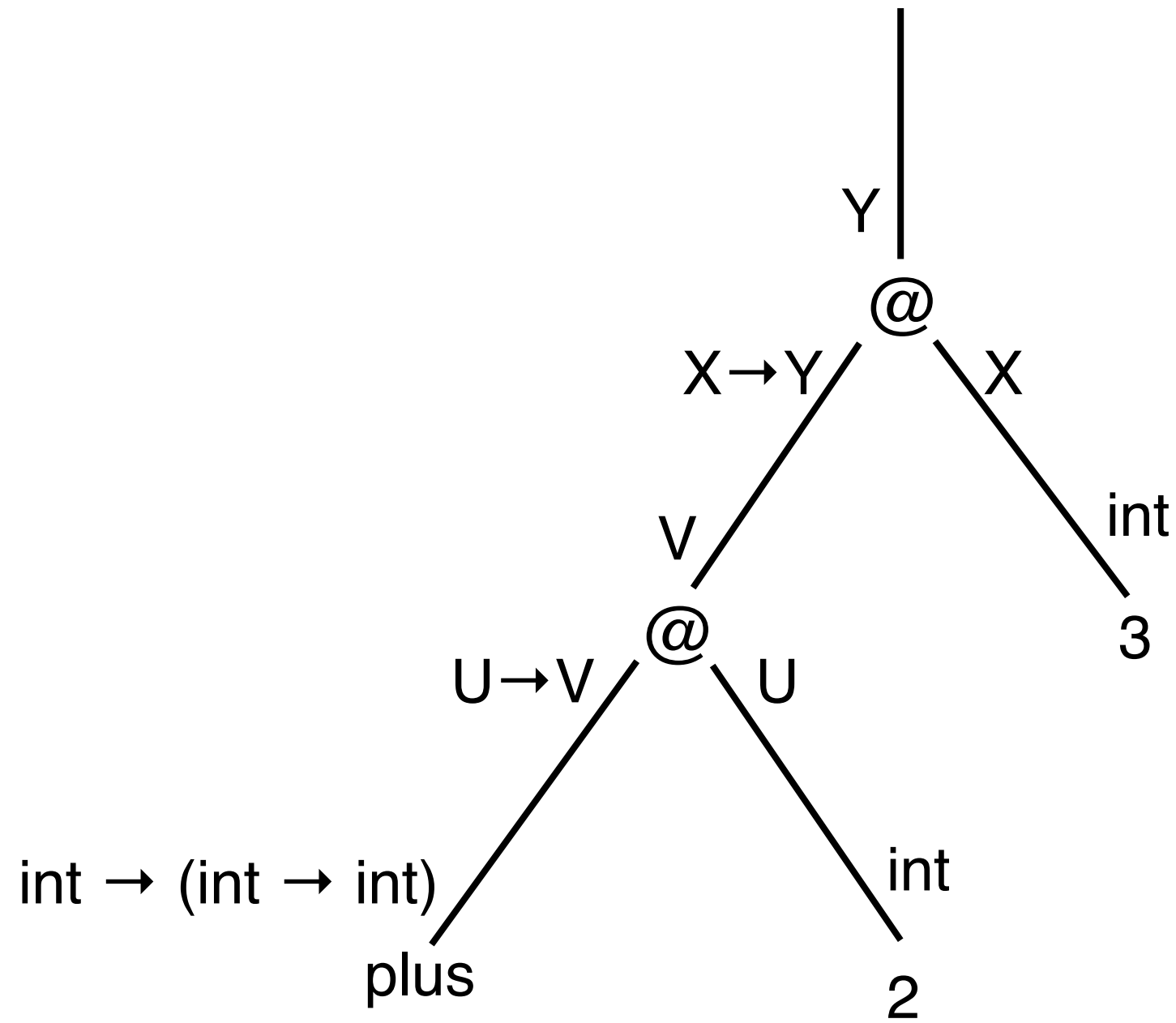


(plus @ 2) @ 3

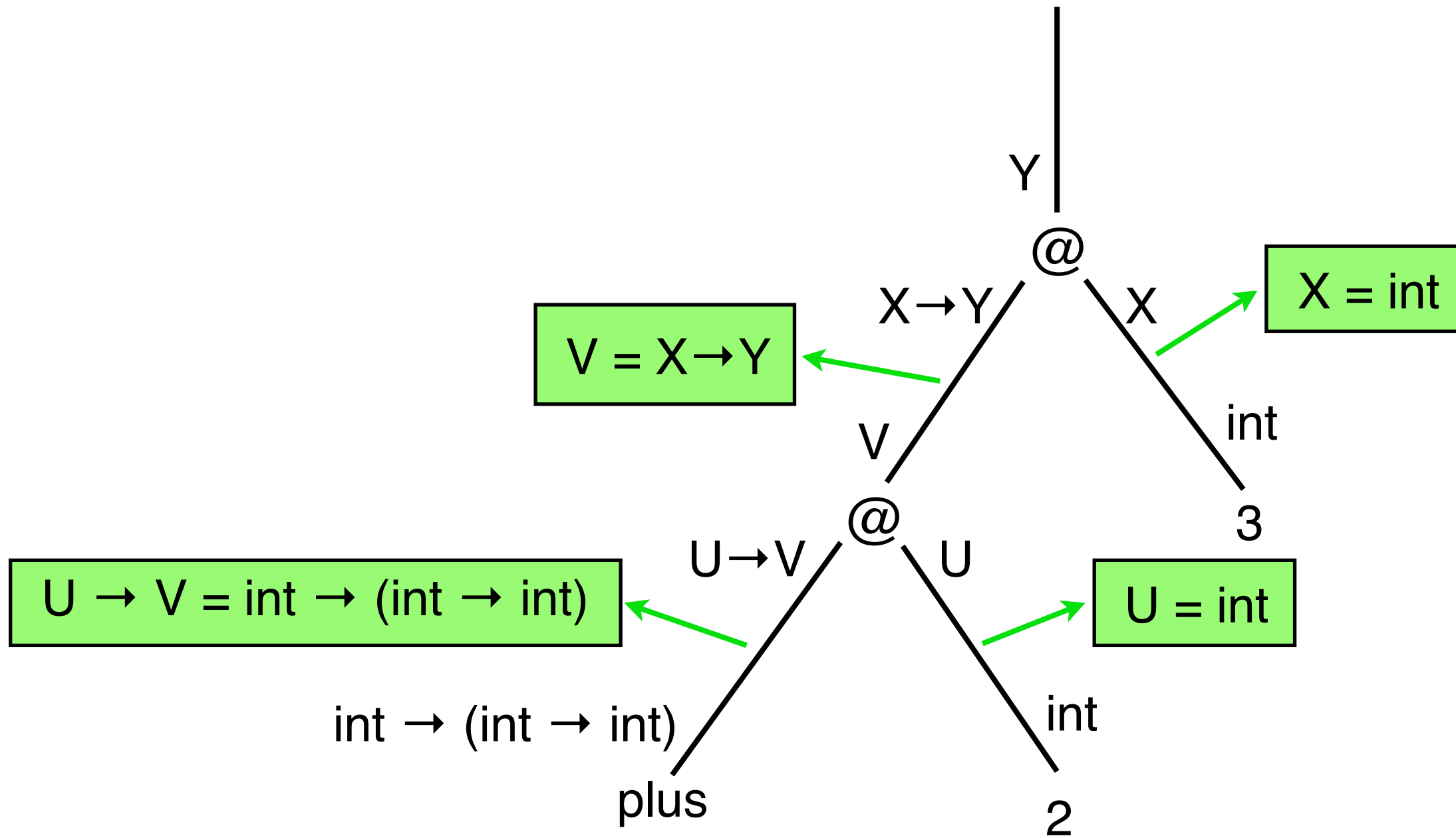


Annotate with types

plus : int $\rightarrow$ (int $\rightarrow$ int)

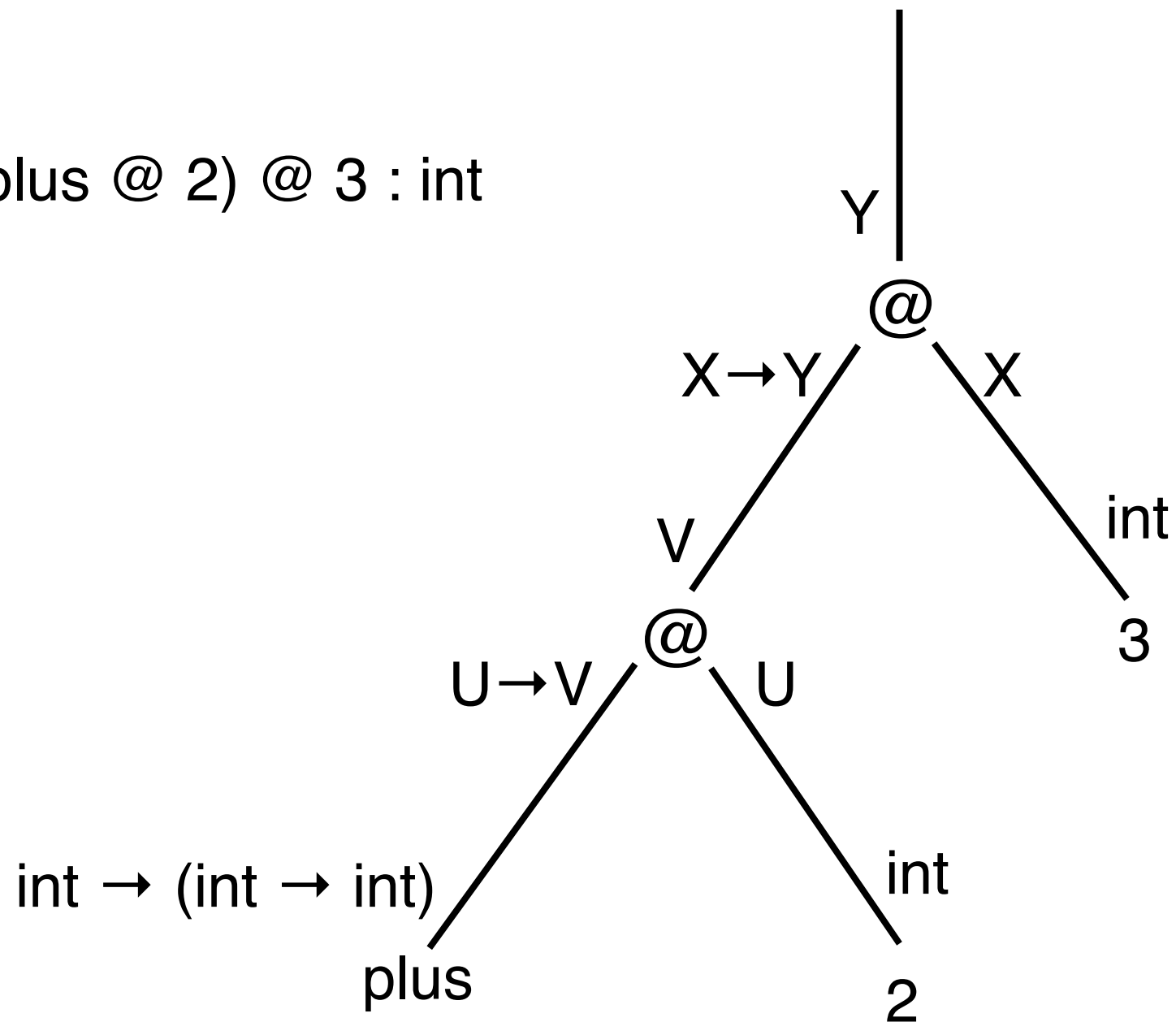


plus : int $\rightarrow$ (int $\rightarrow$ int)



plus : int $\rightarrow$ (int $\rightarrow$ int)

I- (plus @ 2) @ 3 : int



X = int

U = int

V = X $\rightarrow$ Y

U $\rightarrow$ V = int $\rightarrow$ (int $\rightarrow$ int)



unification

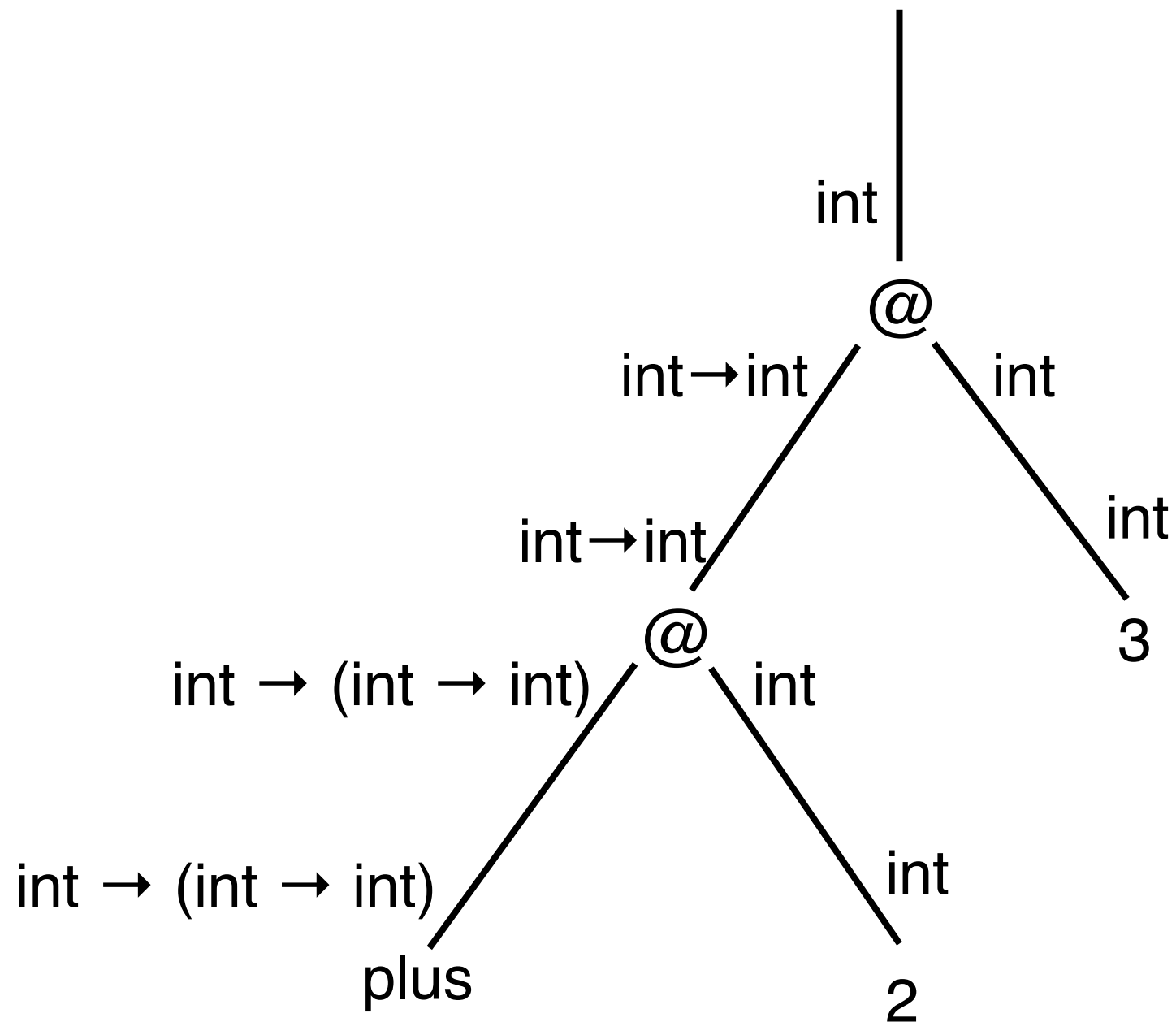
X = int

U = int

V = int $\rightarrow$ int

Y = int

$\Gamma = \text{plus} : \text{int} \rightarrow (\text{int} \rightarrow \text{int})$



$X = \text{int}$
 $U = \text{int}$
 $V = \text{int} \rightarrow \text{int}$
 $Y = \text{int}$

$\Gamma \vdash (\text{plus } @ \ 2) \ @ \ 3 : \text{int}$