

## Homework 5

Due: In class on Friday October 15th

Redo the following exercises from the Lectures Notes:

Exercise 2.2.18

Exercise 2.2.19

Exercise 2.2.20

Due: In class on Monday October 18th

Solve the following exercises from the Lecture Notes:

Exercise 4.1.25

Exercise 4.1.32

(1) Give an (a) algebraic (b) combinatorial proof of the property:

$$\binom{a+b}{n} = \sum_{i=0}^n \binom{a}{i} \binom{b}{n-i}$$

(2) Let  $X$  be a set of  $n + 1$  integers such that none are divisible by  $n$ . Prove there exists two elements of  $X$  such that their difference is divisible by  $n$ .

(3) What is the probability that a poker hand (5 cards) does not contain a pair (2 cards of the same kind)?

Solve the following problems from the Text Book, page 320 - 321:

Problem 14

Problem 16